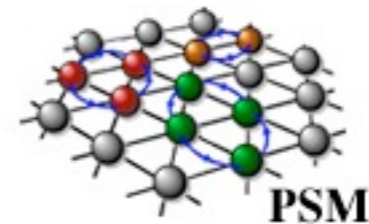


# Spin-charge interplay in frustrated itinerant systems

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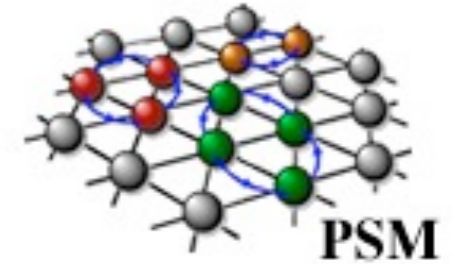
Yukitoshi Motome



**PSM 2010**

INTERNATIONAL SYMPOSIUM ON PHYSICS OF NEW QUANTUM PHASES IN SUPERCLEAN MATERIALS  
MARCH 9-12, 2010 YOKOHAMA, JAPAN

# Partial list of recent activities...



- 📌 Chirality-driven mass enhancement in the kagome Hubbard model (M. Udagawa and YM, Phys. Rev. Lett. **104**, 106409 (2010); [Fig.1 in Abstract](#))
- 📌 Phase competition in the pyrochlore double-exchange model (YM and N. Furukawa, Phys. Rev. Lett. **104**, 106407 (2010); [Fig.2 in Abstract](#))
- 📌 Partial Kondo screening in frustrated Kondo models [**P15 K. Nakamikawa**] (K. Nakamikawa, Y. Yamaji, M. Udagawa, and YM, in preparation)
- 📌 Non-coplanar order and anomalous Hall effect in the triangular-lattice double-exchange model (Y. Akagi and YM, in preparation)
- 📌 ... and more !  
[**P16 H. Ishizuka**; **P17 J. Yoshitake**; **P22 M. Udagawa**; **P43 T. Misawa**]

# Chirality-driven mass enhancement in the kagome Hubbard model

Masafumi Udagawa and Yukitoshi Motome



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## Introduction

- heavy  $d$  electrons: Kondo or correlation + frustration?

## Model and Method

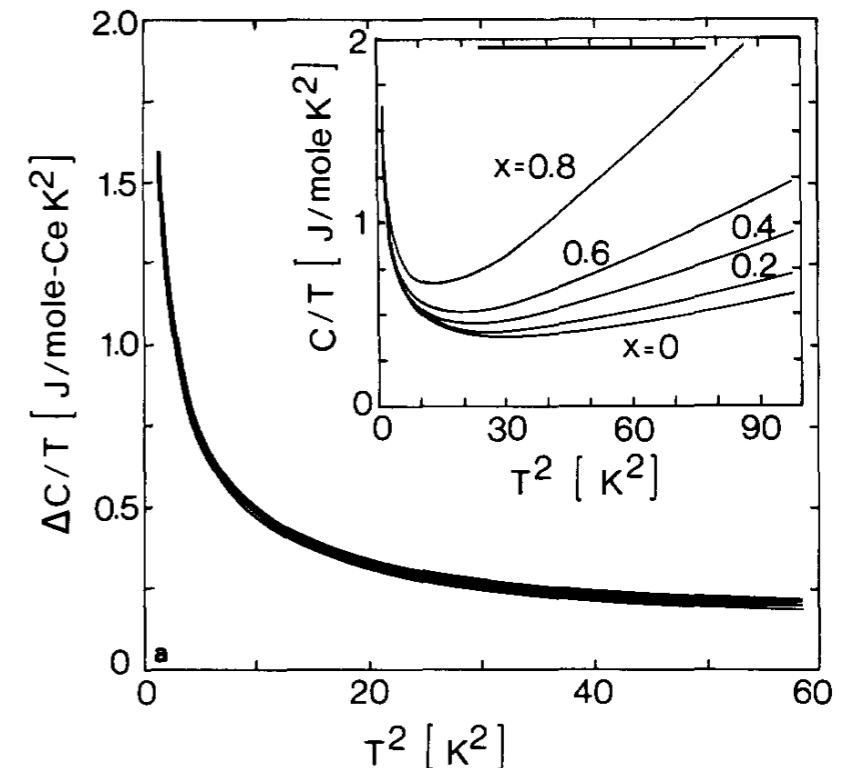
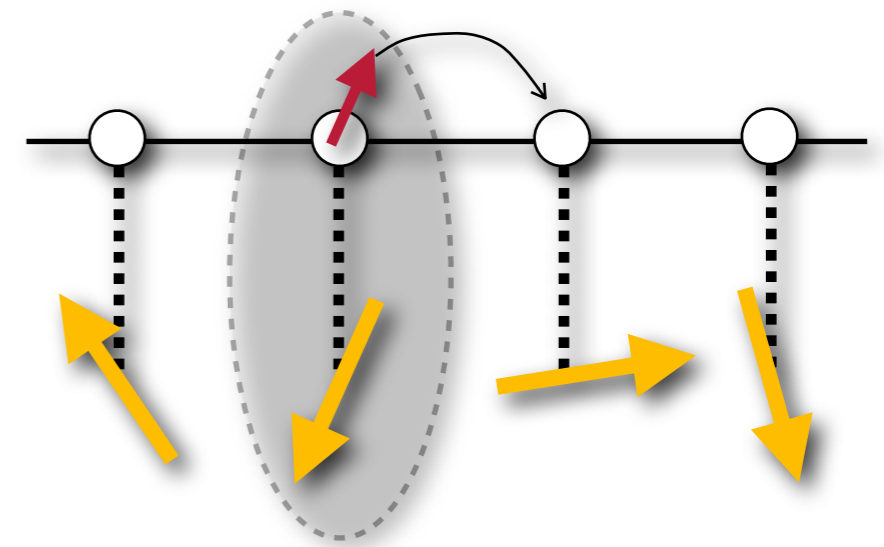
## Results

- energy hierarchy among charge, spin, and chirality
- heavy-mass behavior due to the degeneracy associated with chirality

## Summary

# Heavy mass: Conventional Kondo physics

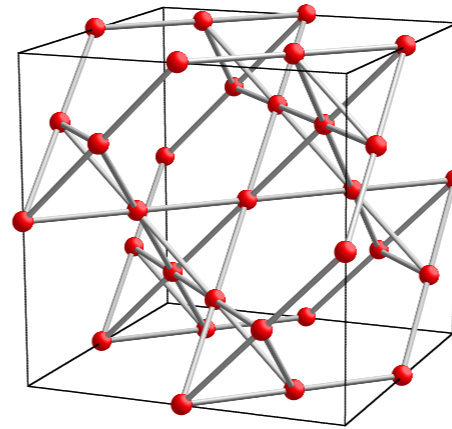
- heavy-fermion *f*-electron systems:  
hybrid of conduction electrons and localized moments
- large mass renormalization due to  
screening of localized spins by conduction electrons at Kondo temperature  $T \sim T_K$ 
  - ➔ release of the spin entropy below  $T_K$
  - ➔ specific-heat coefficient:  
 $\gamma \sim \log 2/T_K$
- ✓ localized moments = entropy reservoir



# Heavy mass in transition metal oxides: Unconventional mass enhancement?

- several examples of heavy  $d$  electrons

$\text{LiV}_2\text{O}_4$ ,  $(\text{Y}_{1-x}\text{Sc}_x)\text{Mn}_2$ ,  $\beta\text{-Mn}$ , ...



- typical: spinel oxide  $\text{LiV}_2\text{O}_4$

- frustrated pyrochlore lattice of V
- no clear sign of phase transition
- characteristic temperature  $T^* \sim 20\text{-}30\text{K}$ :  
heavy mass behavior at lower  $T$

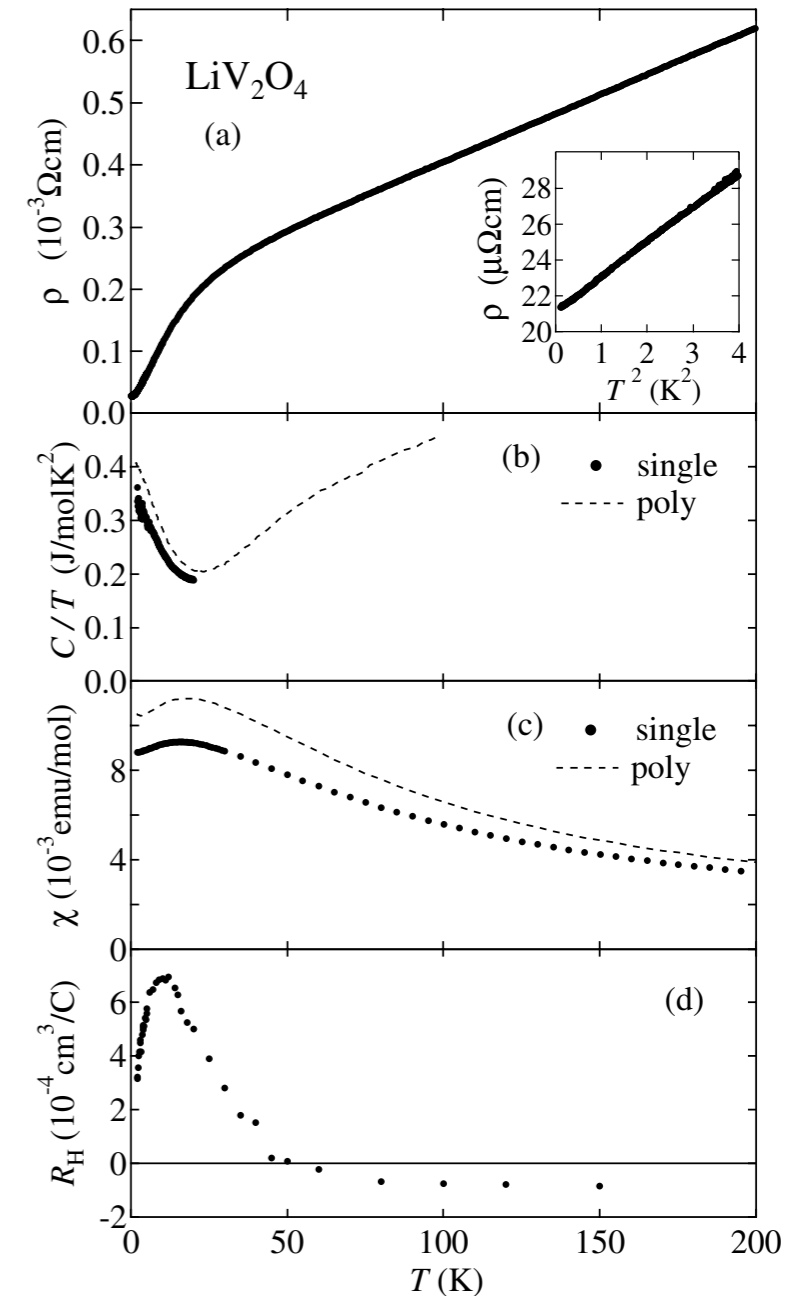
- controversial on the mechanism of heavy mass behavior: no obvious entropy reservoir

*Kondo ?*

V. I. Anisimov *et al.*, 1999

*electron correlation + frustration ?*

V. Eyert *et al.*, 1999; H. Tsunetsugu, 2002; Y. Yamashita and K. Ueda, 2003, etc.

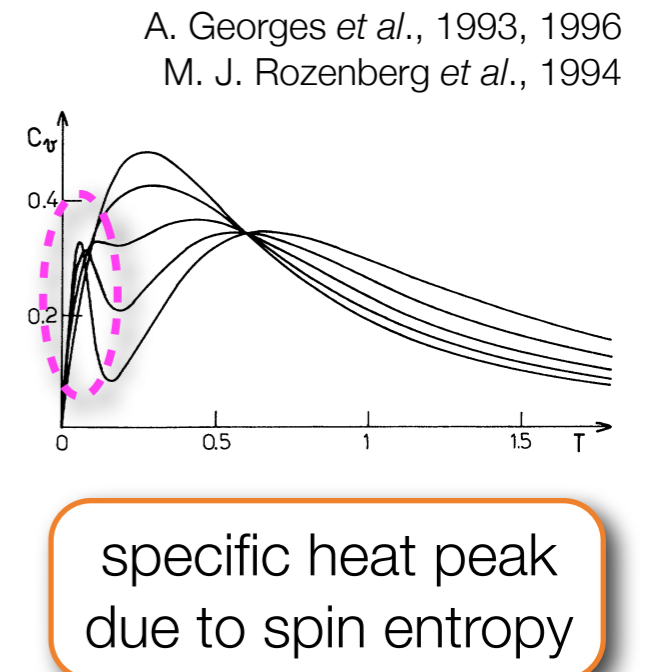
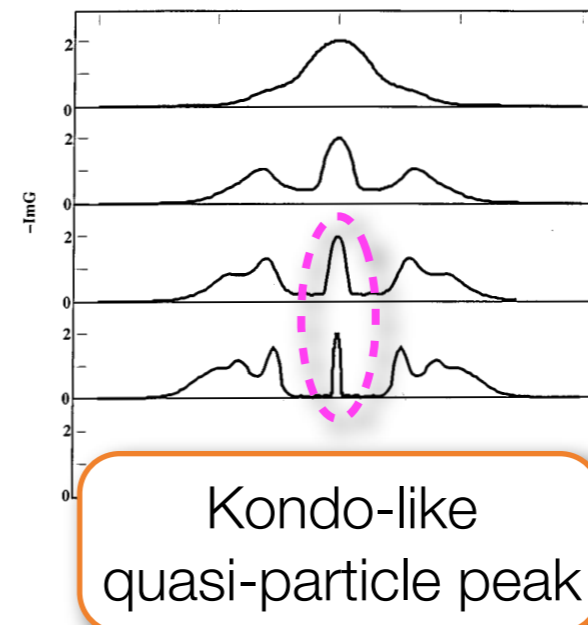
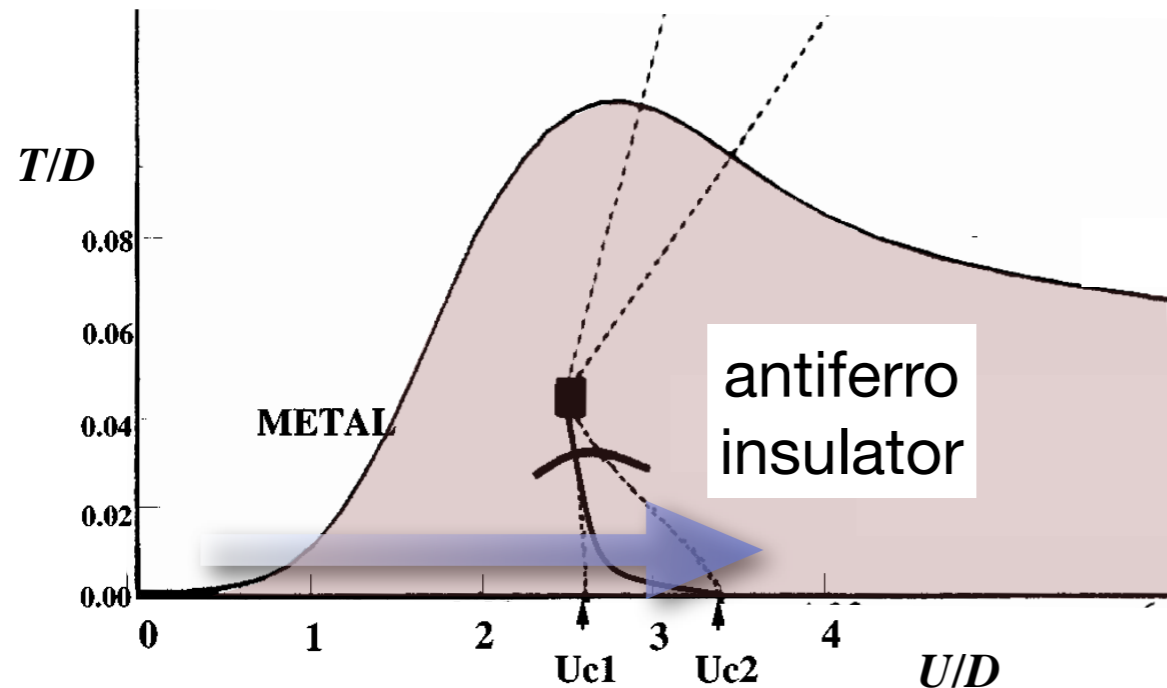


J. Kondo *et al.*, 1999

C. Urano *et al.*, 2000

# Electron correlation + Frustration: A “folklore”

- Mott criticality (Brinkman-Rice, Gutzwiller, dynamical mean-field, ...)

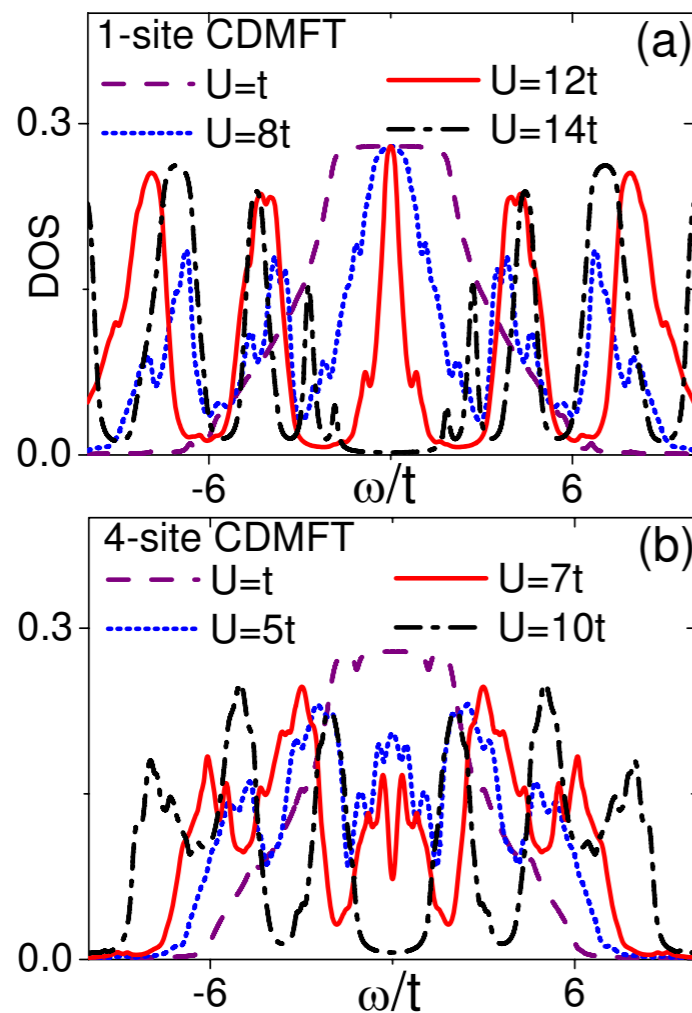


- ✓ critical mass enhancement in the paramagnetic solution
- ✓ local spin fluctuation under strong correlation = entropy reservoir
- ✓ Usually, all of these are masked by the symmetry breaking

- “Folklore”: Frustration suppresses the symmetry breaking and rejuvenates the mass enhancement hidden in the ‘bare’ paramagnetic state.

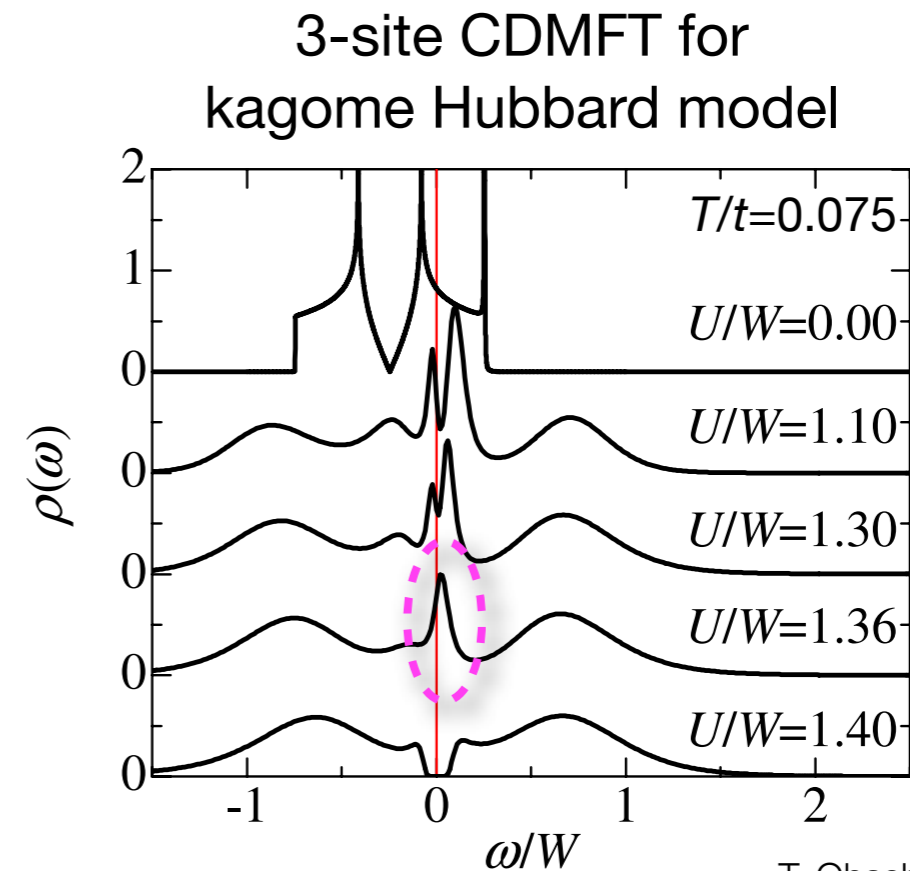
# Caveat...

- Even in the paramagnetic solution, the quasi-particle peak is fragile against spatial correlations.



Y. Z. Zhang and M. Imada, 2007

- On the other hand, in the frustrated case...



T. Ohashi *et al.*, 2006

What is the 'true' role of frustration?

# Objectives

---

- to clarify the role of frustration in correlated metals
  - secondary role, just to suppress the spatial correlations ?
    - ➔ If yes, mass enhancement occurs in the energy scale of spin  $\sim J$
  - The answer is NO ! (as we will see later)
    - ➔ mass enhancement occurs at much smaller energy scale
  - What determines the smaller new energy scale ?
    - ➔ emergent degree of freedom under frustration + correlation
  
- to explore the new mechanism of quasi-particle mass enhancement



# Model and Method

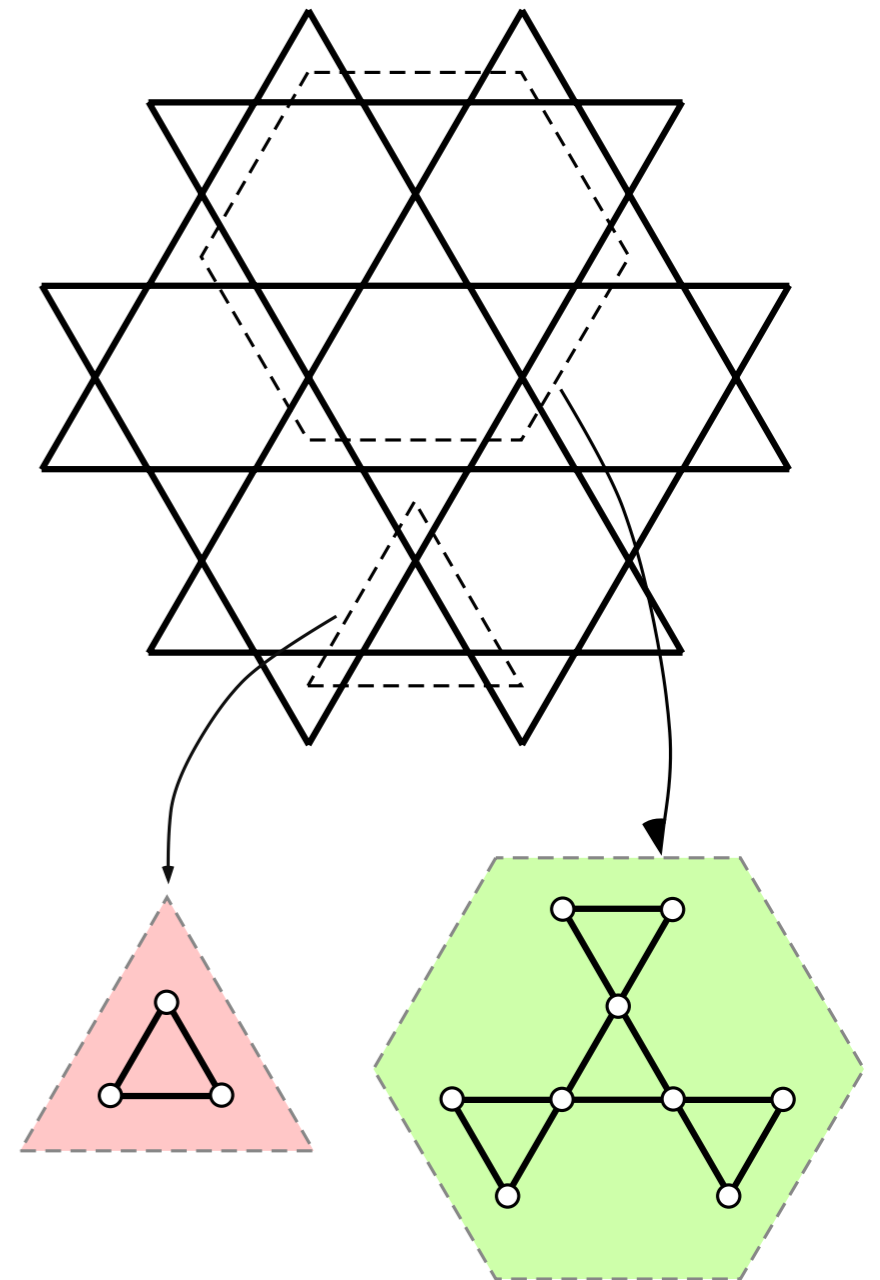
- Hubbard model on the kagome lattice at half filling

$$\mathcal{H} = -t \sum_{\langle ij \rangle \sigma} (c_{i\sigma}^\dagger c_{j\sigma} + \text{h.c.}) + U \sum_i n_{i\uparrow} n_{i\downarrow}$$

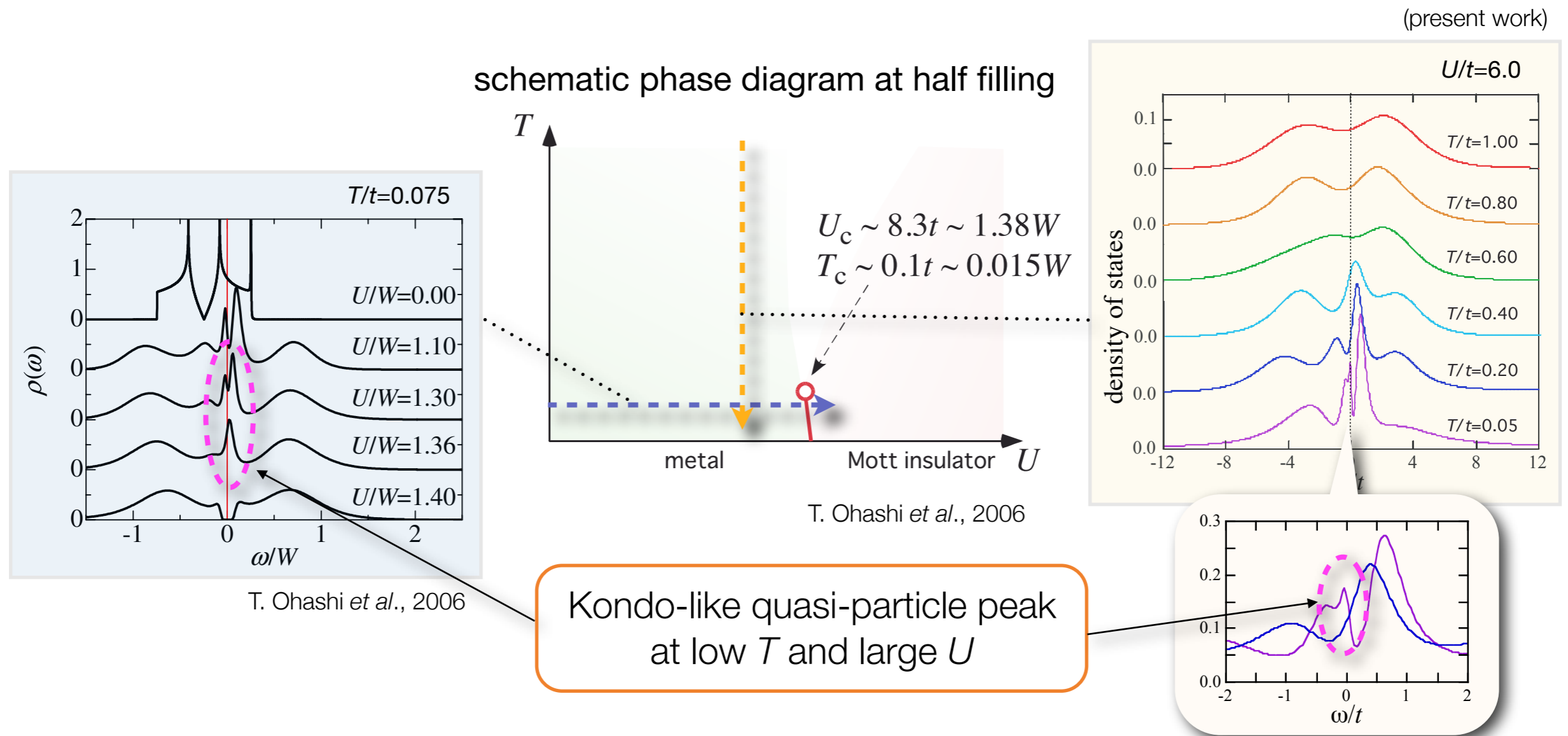
- a minimal model including both electron correlation and frustration (Y. Imai *et al.*, 2003; N. Bulut *et al.*, 2005; T. Ohashi *et al.*, 2006; B. H. Bernhard *et al.*, 2007)
- Mott transition at  $U_c \sim 8.3t$  (T. Ohashi *et al.*, 2006)

- cluster extension of the dynamical mean-field theory

- mapping to cluster impurity models (3 or 9 sites)
- impurity problem solver: continuous-time quantum Monte Carlo method (E. Gull *et al.*, 2008)



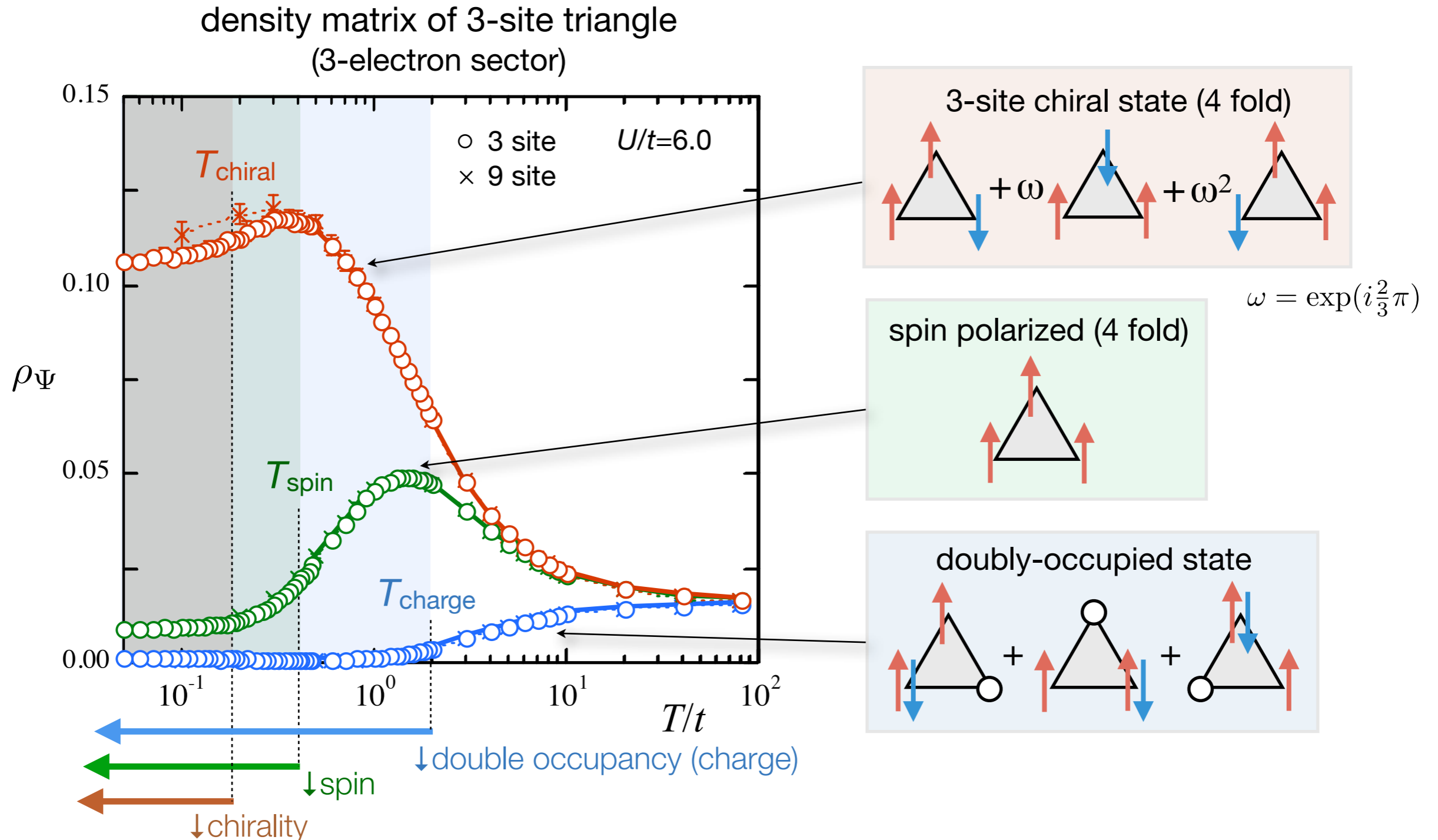
# Result: Heavy-fermion behavior



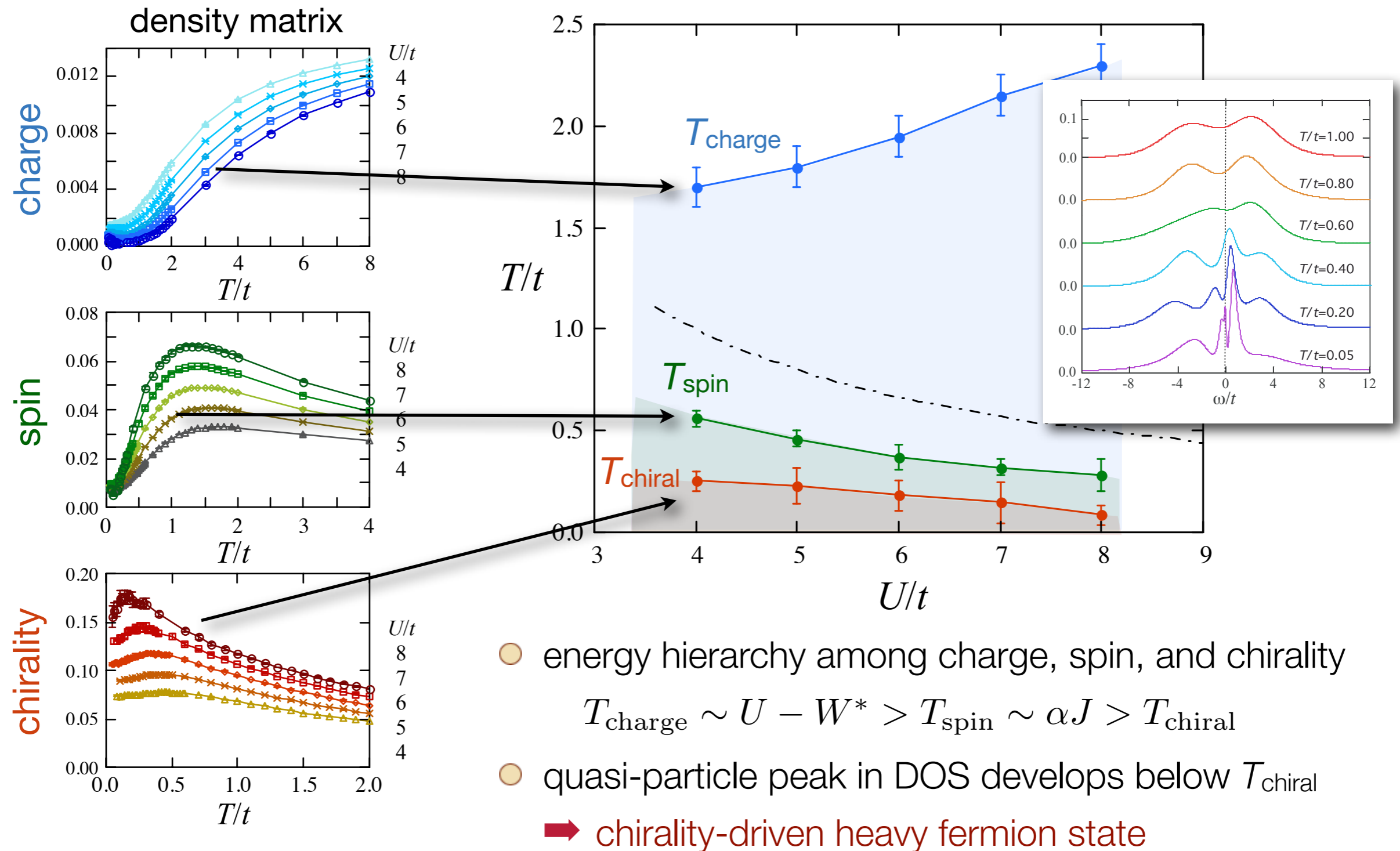
- To identify the relevant degree of freedom, we calculate density matrix = prob. distribution of quantum mechanical states

$$\rho_{\Psi} = \frac{1}{Z} \text{Tr} |\Psi\rangle \langle \Psi| e^{-\beta \mathcal{H}}$$

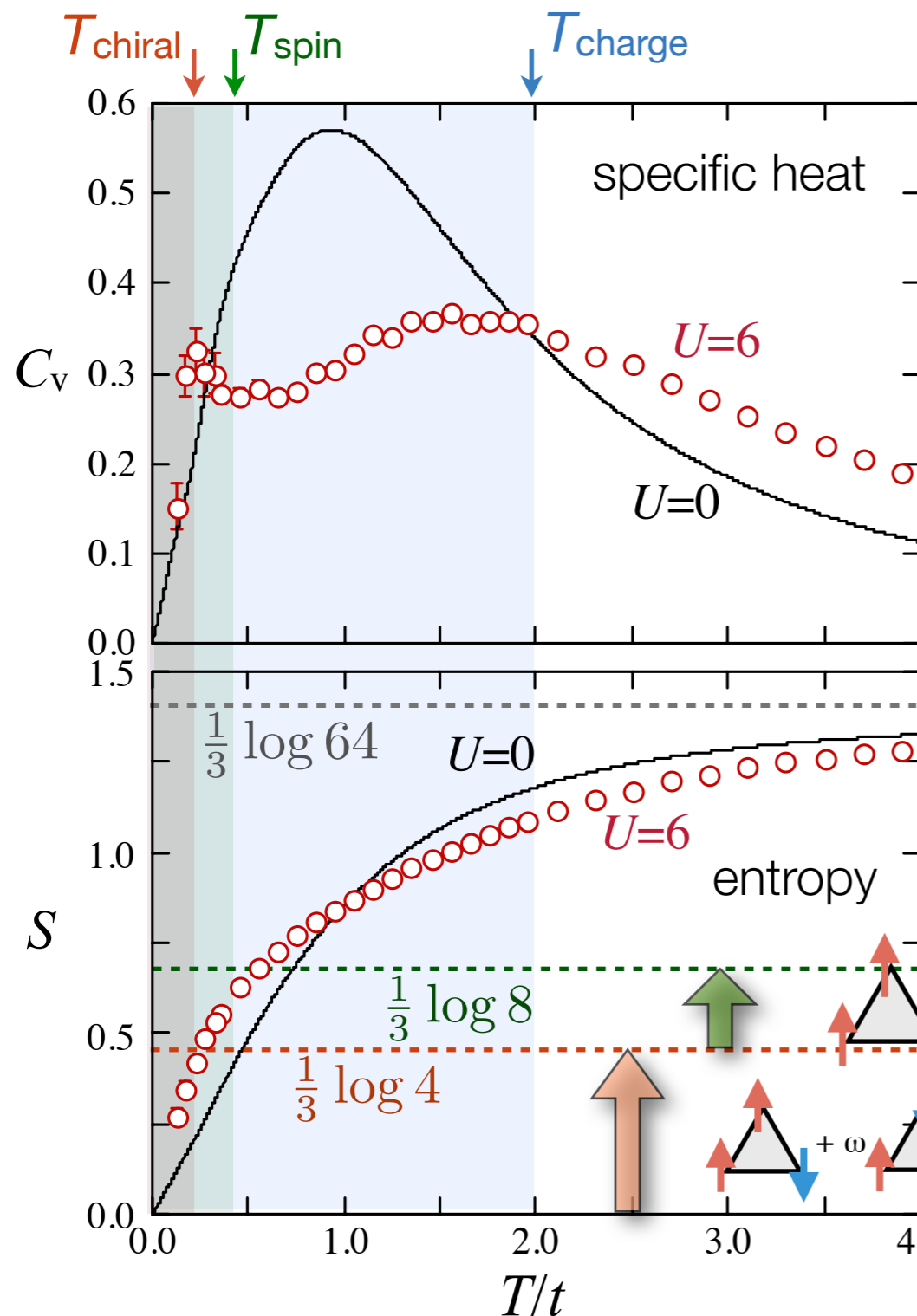
# Result: Spin chirality degree of freedom



# Result: Crossover temperatures

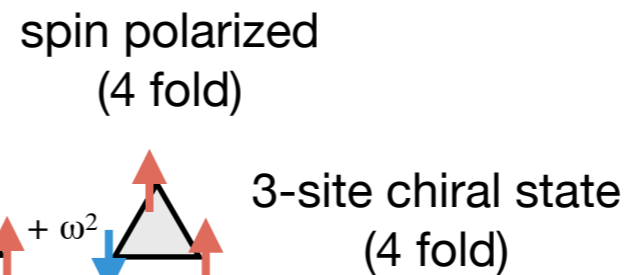


# Result: Specific heat and entropy



- charge-spin-chirality separation
  - broad hump in  $C_v$  at  $T \sim T_{\text{charge}}$
  - entropy  $\sim \log 8$  at  $T \sim T_{\text{spin}}$
  - sharp peak in  $C_v$  and entropy  $\sim \log 4$  at  $T \sim T_{\text{chirality}}$
- chirality-driven mass enhancement
  - specific-heat coefficient:

$$\gamma \simeq \frac{1}{3} \log 4 / T_{\text{chiral}}$$

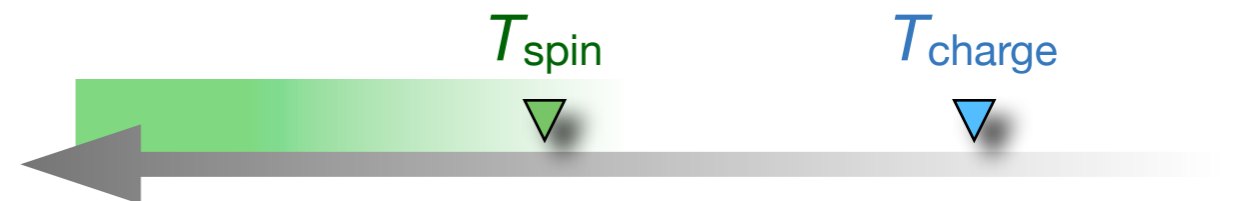


# Discussion

## ■ “Folklore” scenario

Frustration just suppresses magnetic LRO

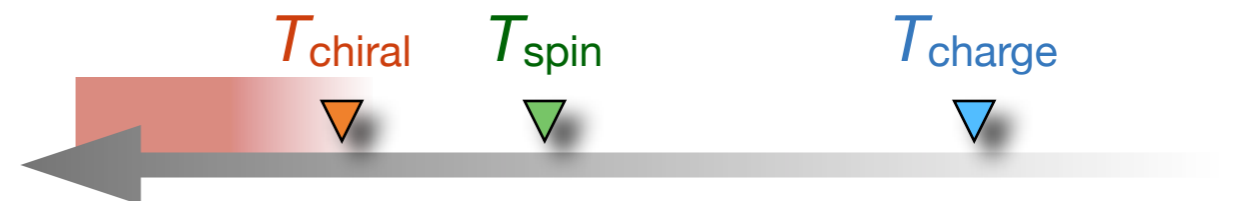
➡ heavy mass due to spin entropy



## ■ Present mechanism

Frustration brings about **an emergent degree of freedom, chirality**

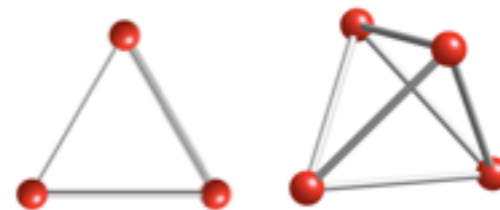
➡ heavy mass due to spin chirality



## ○ heavy-mass behavior:

crossover from **highly-symmetric local state** to **renormalized Fermi liquid**

emergent composite objects  
with high local symmetry



chirality, multipole, etc.

# Summary

M. Udagawa and YM, Phys. Rev. Lett. **102**, 106409 (2010)

- cellular DMFT study of correlated metallic region in the kagome Hubbard model
  - ✓ continuous-time QMC
  - ✓ cluster-size dependence
- Emergent degree of freedom, chirality, plays a decisive role at low  $T$ .
  - ✓ energy hierarchy
  - ✓ sharp peak in the specific heat
  - ✓ mass enhancement
- Our results uncover an intensive role of geometrical frustration in correlated metal (not secondary just to suppress LRO).

