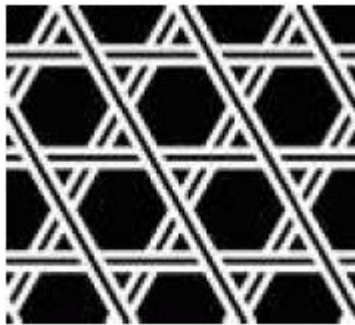


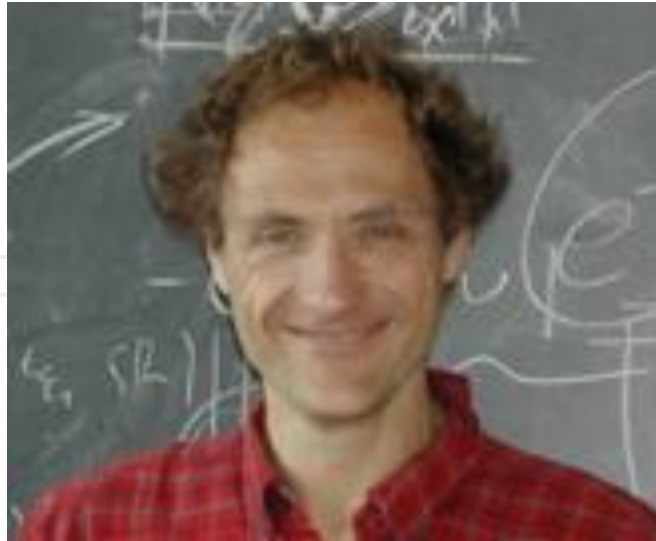
Exotic Antiferromagnets on the kagomé lattice: a quest for a Quantum Spin Liquid

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Physics of New Quantum Phases in Superclean Materials (PSM2010)
Yokohama, Japan (March 9 -12, 2010)



Laura Messio (Ph.D student)

Philippe Sindzingre

Grégoire Misguich IPhT Saclay

J.C. Domenge (Ph. D student *Not shown*)

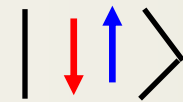
Outline

- Spin liquids and exotic antiferromagnetic phases: some definitions (parallel with quantum liquids)
- Spin-1/2 Heisenberg model on the kagome lattice : VBC, Critical Spin Liquid or a quantum critical point?
- Herbertsmithite: a quasi perfect Heisenberg model on the kagome lattice?
- Other real compounds on the kagome lattice: Volborthite (*Hiroi et al.*), Cutitmb (*Narumi et al. Europhys. Lett. 2004*), Kapellasite (*A. Wills, B. Fak, 2010*) are not pure n.n. Heisenberg models... but may harbor exotic chiral phases (*Messio 2010*)
- A first order chiral transition at $T \neq 0$: the role of Z_2 vortices (*J.-C. Domenge, PRB 77 2008, L. Messio & P. Viot. PRB 78 2008*)

Exchange interaction : W. Heisenberg

$$H_{i,j} = \mathbf{S}_i \cdot \mathbf{S}_j$$

- the “classical ground-state”: $|-,+\rangle$
is a symmetry breaking state



- the quantum ground-state does not break SU(2):
 $|0\rangle = [|+, -\rangle - |-, +\rangle] / \sqrt{2}$ called a Valence Bond st.



- The variational energy of the classical state reduces to:

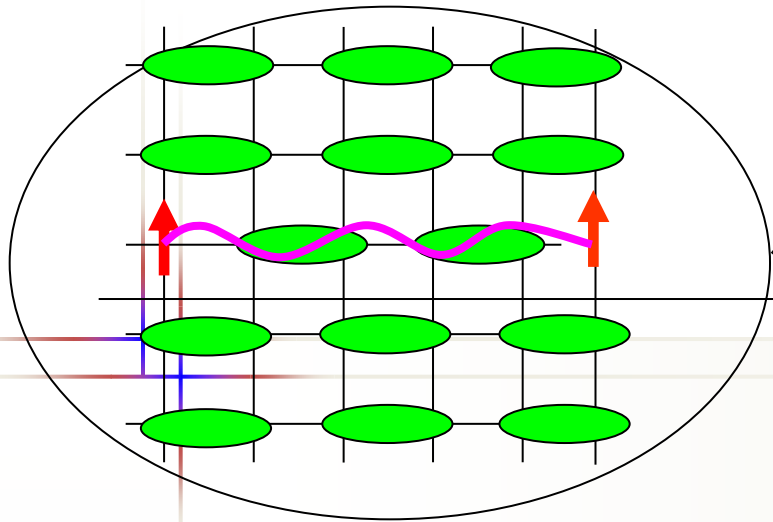
$$E_{cl} = \langle +, - | H_{i,j} | +, - \rangle = \langle +, - | S_i^z, S_j^z | +, - \rangle = -1/4$$

whereas:

$$\begin{aligned} E_{qu} &= \langle 0 | S_i^z, S_j^z | 0 \rangle + \frac{1}{2} [\langle 0 | S_i^+, S_j^- | 0 \rangle + \langle 0 | S_i^-, S_j^+ | 0 \rangle] \\ &= \text{the “classical energy”} + \text{“energy gain due to quantum fluctuations”} \\ &= -1/4 + (-1/2) \\ &= \langle \text{potential energy term} \rangle + \langle \text{kinetic energy term} \rangle \end{aligned}$$

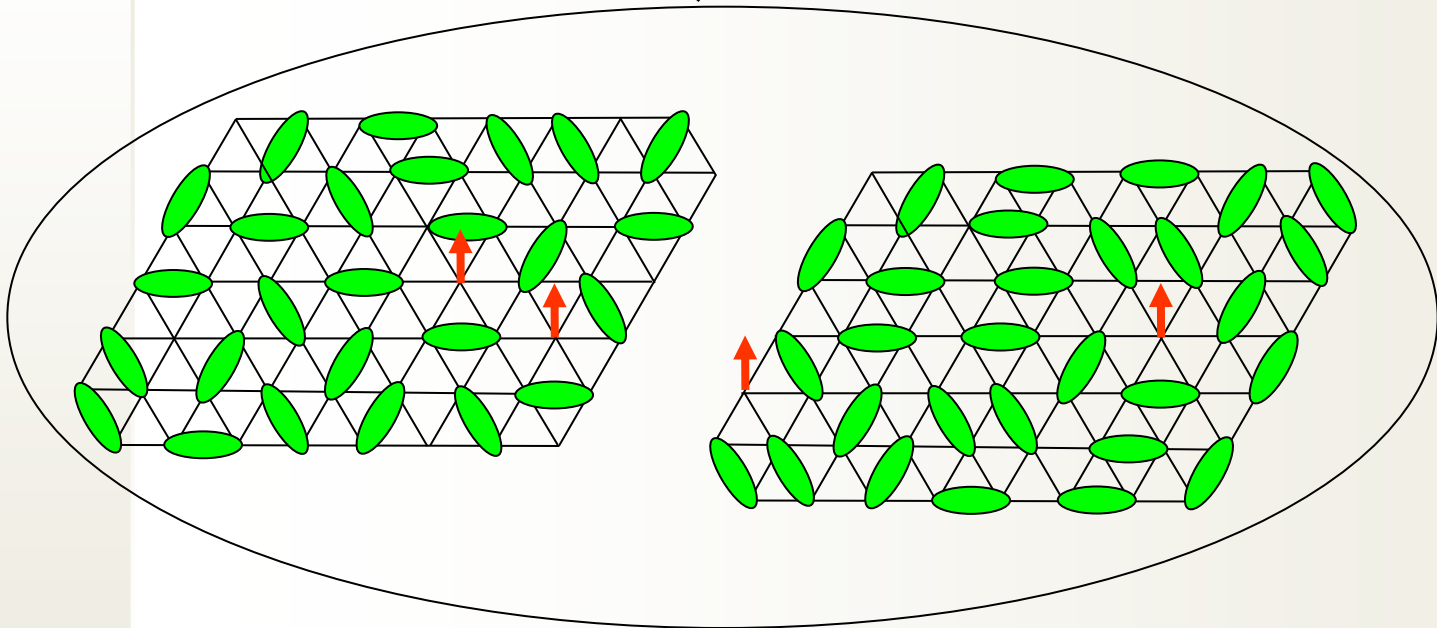
What do theoreticians call Quantum Spin Liquids ?

- A magnetic spin system with NO LRO in ANY local order parameter at $T=0$ and no symmetry breaking.
- Rather rare situation! Most magnets are “solid” like!
 - Colinear or non colinear Néel magnets have on site magnetizations
 - Nematic magnets : 4-spin ring exchange on square lattice -> nematic magnets: *Laeuchli et al, PRL 2005, Shannon, Momoi, Sindzingre 2005 on the triangular lattice , Momoi, Shannon ,Sindzingre 2006* -> quadrupolar or octupolar order
 - Valence Bond Crystals (*Shastry Sutherland, Fouet et al. 2003*) have long range order in singlet bonds.
- with gapless or gapful $\Delta S = 1$ wave-like excitations
- Z_2 gapped spin Liquids: with unconfined $\Delta S = 1/2$ excitations, do exist in theoretical toy models, topological g.s. degeneracy, q-bit toy models. *Misguich et al 98, 99 , Moessner & Sondhi 98, 99, Balents, Fisher and co-workers. Experimental realisation? 2-d ^3He ?*



confined spinons in the
V-B crystal

unconfined spinons in
the R.V.B. Spin Liquids



Classical & Quantum Heisenberg Hamiltonian on the kagomé lattice

$$\begin{aligned} H &= \sum S_i \cdot S_j \\ &= \frac{1}{2} \sum_{\alpha} S_{\alpha}^2 + \text{Cst} \end{aligned}$$

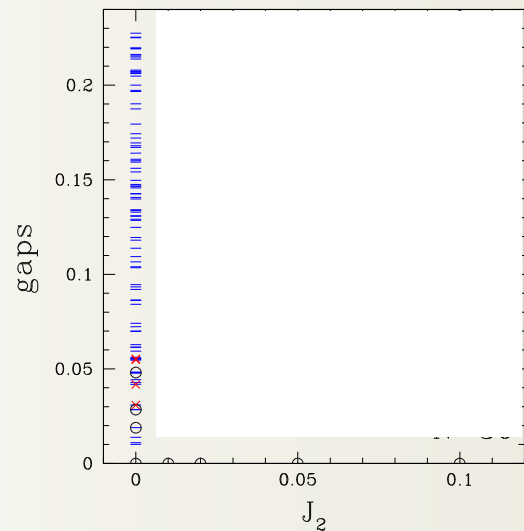
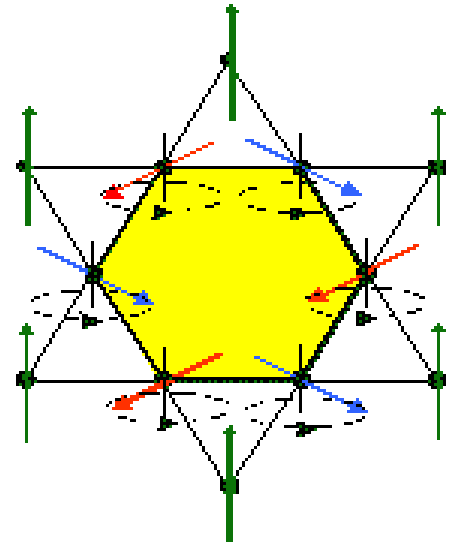
An infinite number of soft modes, an infinite T=0 degeneracy

J. Chalker, et al 92, Huse & Rutemberg 92, Reimers & Berlinsky 93

Quantum spectrum of excitations of N=36 spin-1/2 molecule: good ingredients for a spin liquid behavior, no local order parameter, discretization of energy $\sim 10^{-3}$...

Lecheminant & al. 97, Waldtmann & al. 99

Is it a large enough size to extrapolate to an infinite lattice?





Shores & Nocera 2005

Bert & Mendels group Orsay 2007

Y. S. Lee group MIT 2007

Imai et al. Mac Master Univ. 2007-2008

S.H. Lee group

- Curie-Weiss temperature $\Theta_{\text{CW}} = -300$ K
 - No magnetic order down to 50 mK
 - Dynamical features down to 50 mK
 - No observable gap down to 0.1 meV
 - No SG transition

A Spin Liquid phase down to $T \leq J/4000$

Role of impurities ? Dzyaloshinskii Moriya interactions?

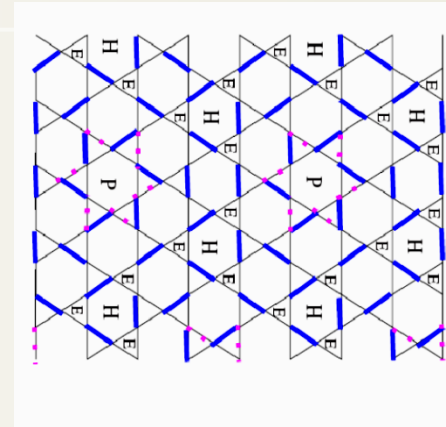
Quantum Spin Liquid on the kagome lattice? *controversies amongst theoreticians*

- Heisenberg model on the kagomé lattice :

- *A Valence Bond Crystal ?*

RRP Singh & D. Huse 2007,

A small gap and a very large unit cell



- *An algebraic spin liquid: Ran, Hermele et al. 2007-2008,*
An extended gapless phase with fermionic spin-1/2 excitations

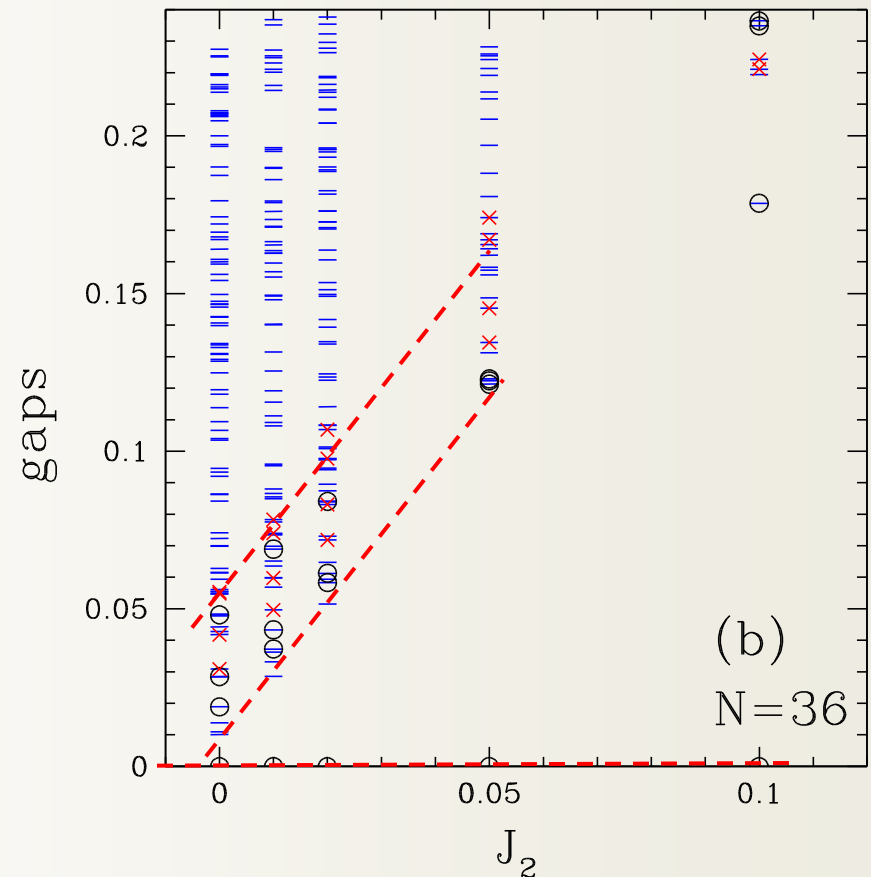
- *A vortex spin liquid: S. Ryu, Motrunich, Alicea & MPA Fisher*
2007 (XY model)

The Heisenberg model on the kagomé lattice: a Spin Liquid near a Quantum Critical Point?

P. Sindzingre & C.L: EPL 88 2009, [arXiv:0907.4164/v2](https://arxiv.org/abs/0907.4164)

- Instability of a putative VBC or of Hermele S.L.
- No intrinsic low energy scale $3 \cdot 10^{-3}$ for $N=36$...

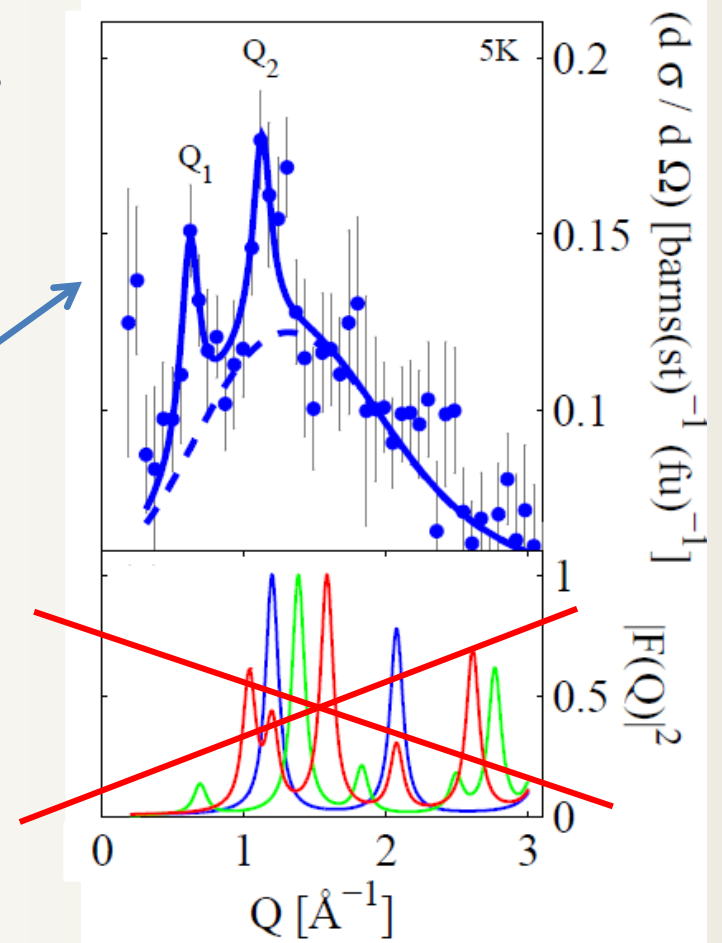
Could it be the signature of a QCP?



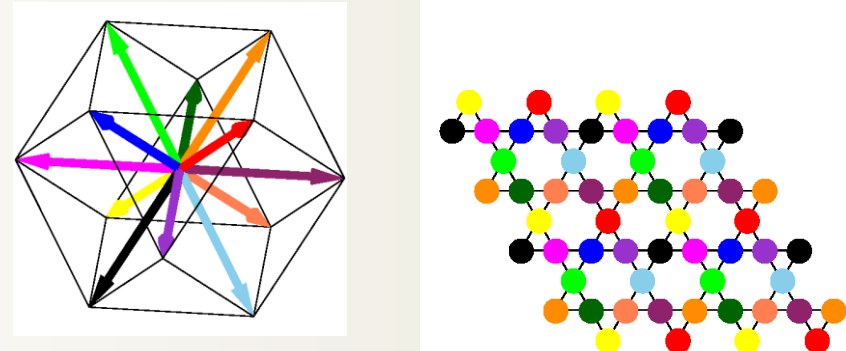
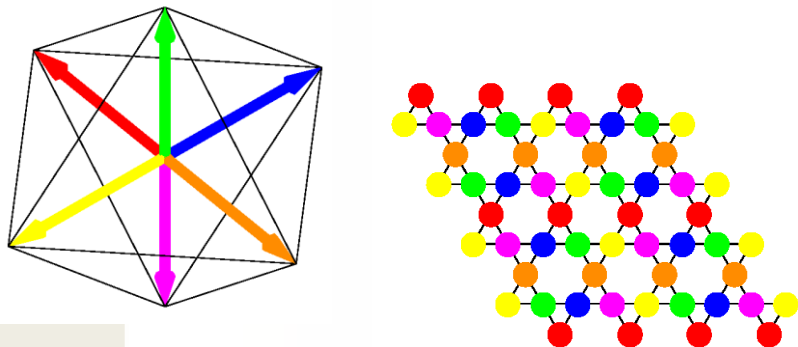
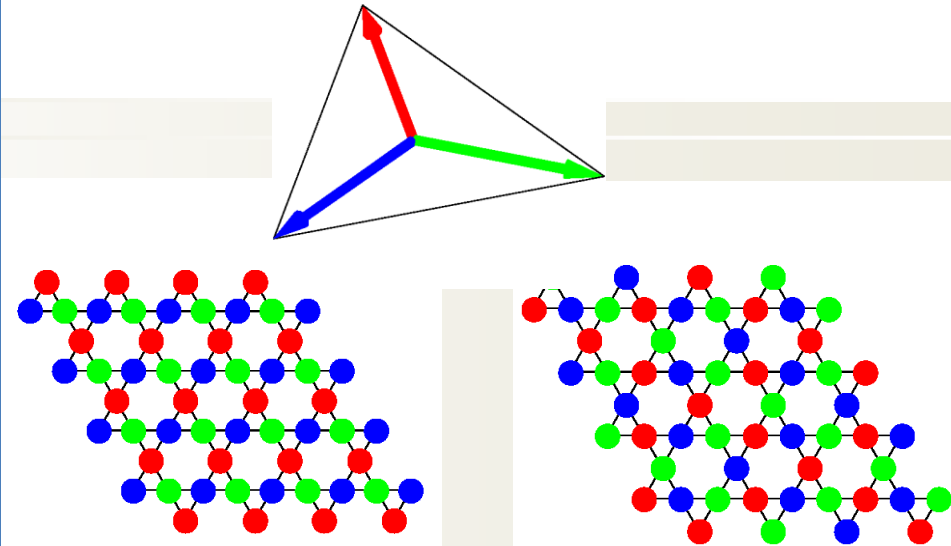
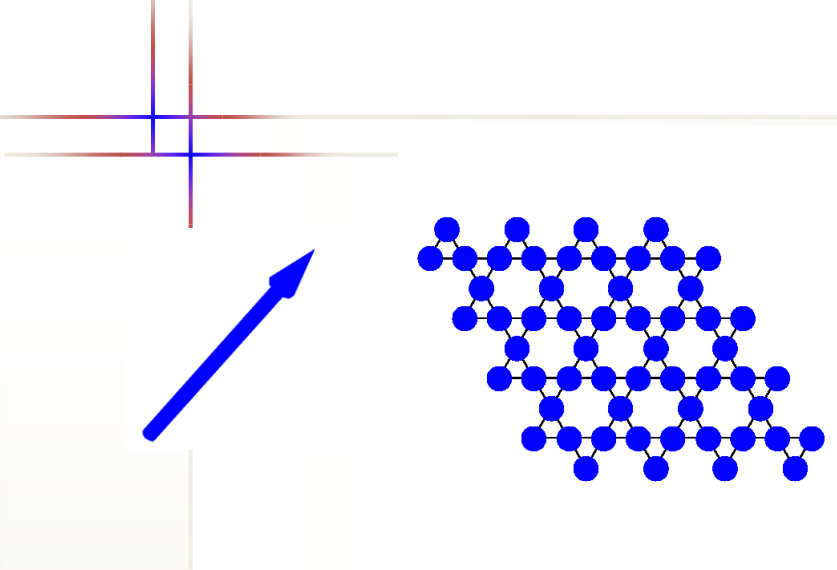
Other “real compounds” on the kagome lattice: Volborthite
(*Hiroi et al.*),
Cutitmb (*Narumi et al. Eur. Lett. 2004*),
Kapellasite (*A. Wills, B. Fak, 2010*)
are not pure n.n. Heisenberg models...

- Experimental indications of non coplanar SRO in Vollborthite

- Z. Hiroi’s group *J. of Phys. Soc. Jpn* 78, 2009,
- G. Nilson & al. (EPFL 2010)
arxiv:1001.2462



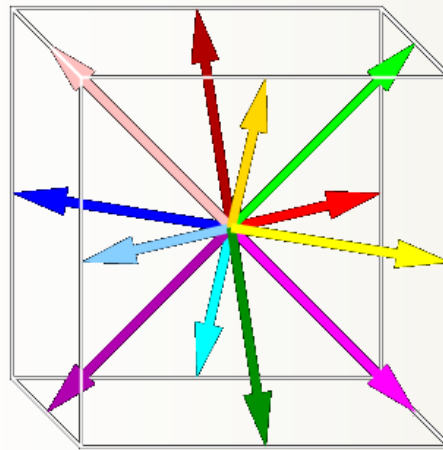
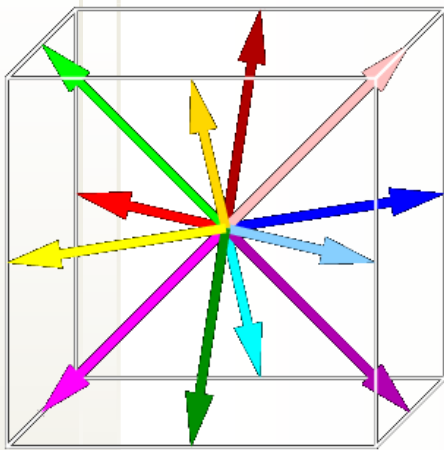
The classical & quantum short range orders on the kagome lattice (PSG analysis, *Messio 2010*)



Chiral sym. breaking in the 12-sublattice cuboc. phase and chiral phase transition

Domenge, Messio & al. PRB 77, 78 2008.

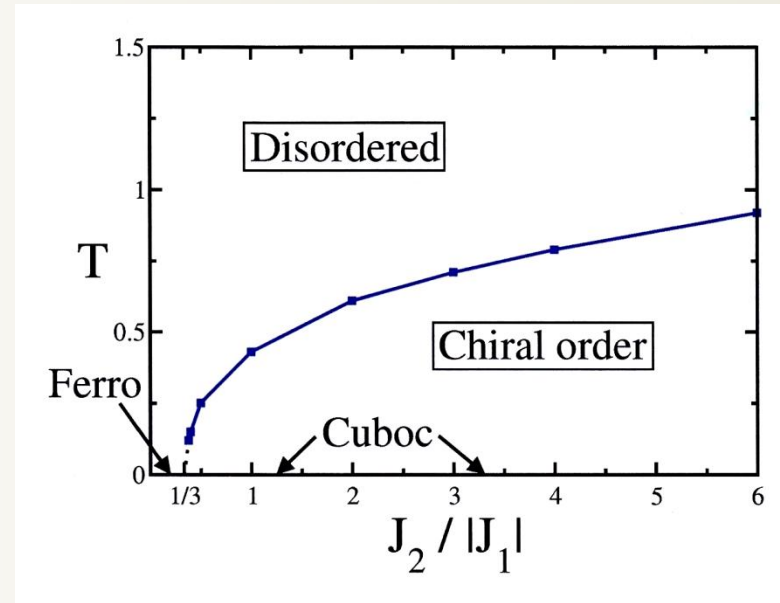
M.C. simulation – class. spins



Scalar
chirality

$\sigma = +1$

$\sigma = -1$

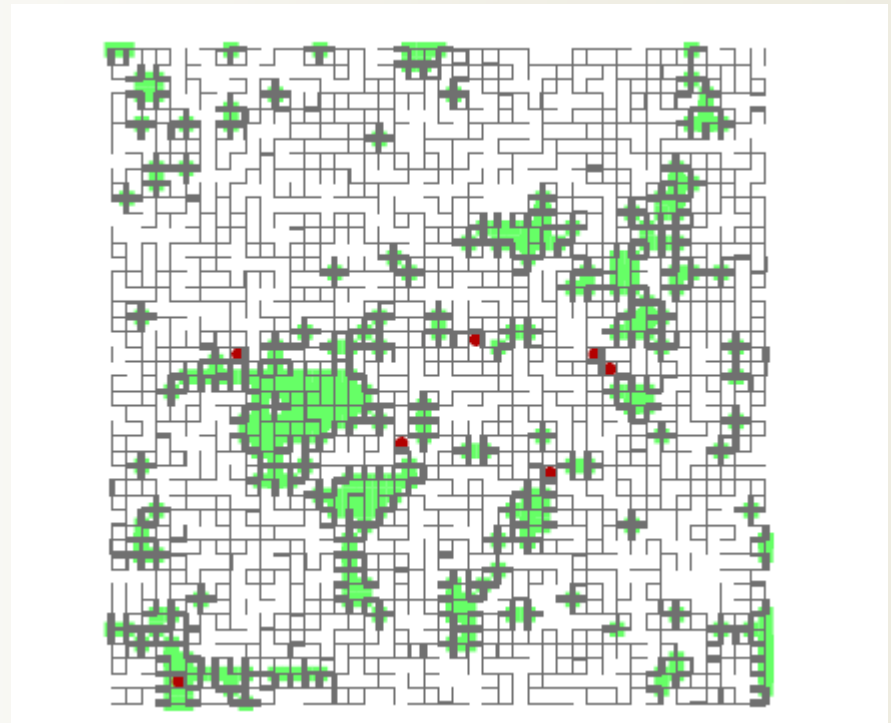


Similar physics in MSE model
Momoi et al PRL 97

Weak universality (Suzuki 1984) ?

First order phase transition mechanism

Snapshot of a spin
chirality configuration
near the phase transition:
 Z_2 vortices (brown points)
nucleate in the domain
walls of chirality
(white/green boundaries)
and modify the domain
wall energy
Messio et al. PRB 78 2008

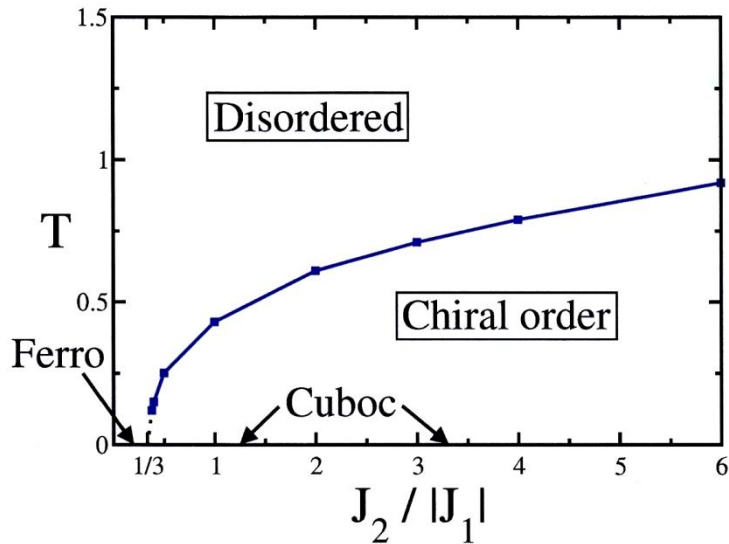


Summary

- Spin liquids and exotic antiferromagnetic phases: some definitions
- Spin-1/2 Heisenberg model on the kagome lattice :
VBC, Critical Spin Liquid **or a system near a Quantum Critical Point?**
(Sindzingre & C.L. 2009)
- Herbertsmithite: a quasi perfect Heisenberg model on the kagome lattice
- Other real compounds on the kagome lattice: Volborthite (*Hiroi et al.*),
Cutitmb (*Narumi et al. Europhys. Lett. 2004*), Kapellasite (*A. Wills, B. Fak, 2010*) are not pure n.n. Heisenberg models... but **may harbor exotic chiral phases** (*Messio 2010*)
- A weakly first order chiral phase transition at $T \neq 0$: **the role of Z_2 vortices** (*J.-C. Domenge, PRB 77 2008, L. Messio & P. Viot. PRB 78 2008*)

T≠0 Phase diagram of the F-AF model

Domenge, Messio et al PRB 2008



The chiral phase transition:

- ✓ weakly first order at small $J_2/|J_1|$ due to Z_2 vortices
- ✓ Going towards criticality when $J_2/|J_1|$ increases

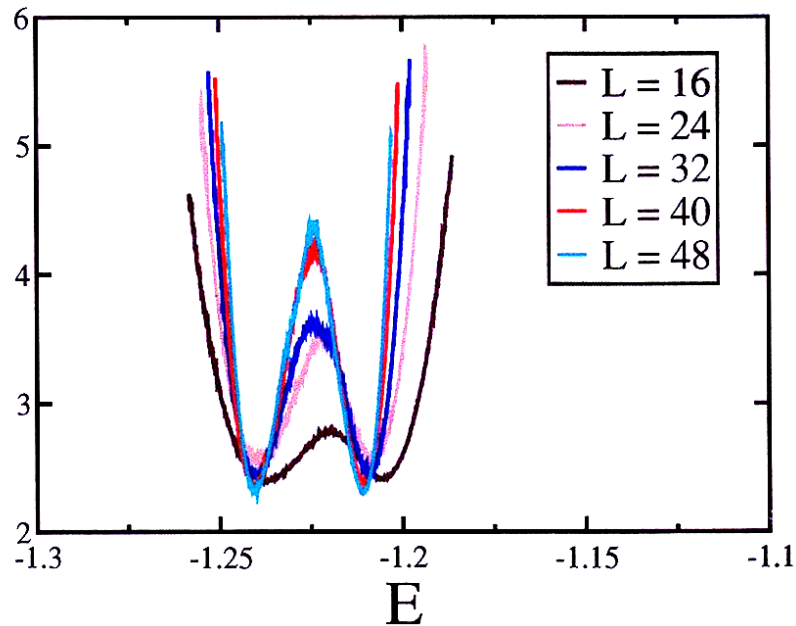
May be not too rare in frustrated magnets

Cyclic 4-spin exchange model *Momoi et al PRL 97*

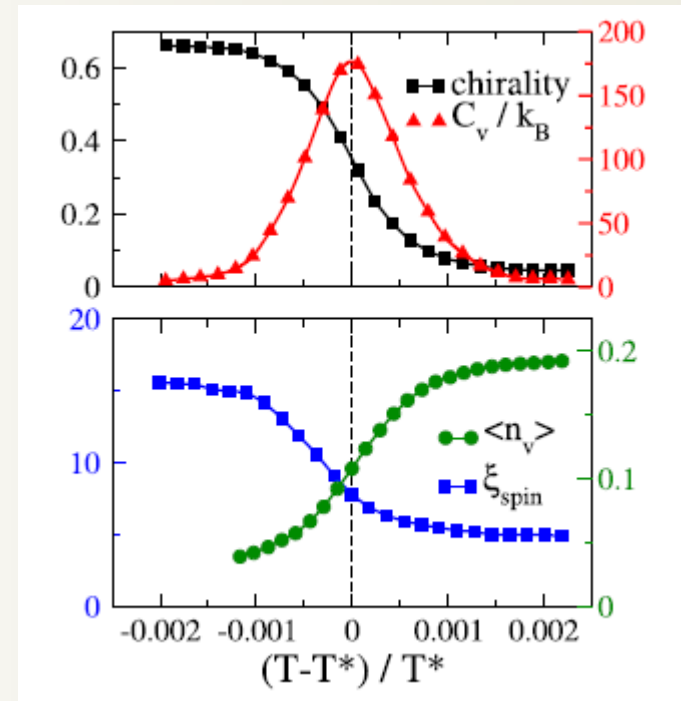
Unfortunately $\text{Cu}_3(\text{titmb})_2(\text{OCOCH}_3)_6 \cdot \text{H}_2\text{O}$ undergoes a ferromagnetic transition at 0.05 Kelvin. (3d effect) Y. Karakı (2008)

As $\gamma\text{-Cu}_2(\text{OH})_3\text{Cl}$ (*Kageyama et al. 2001*)

A very weak first order phase transition

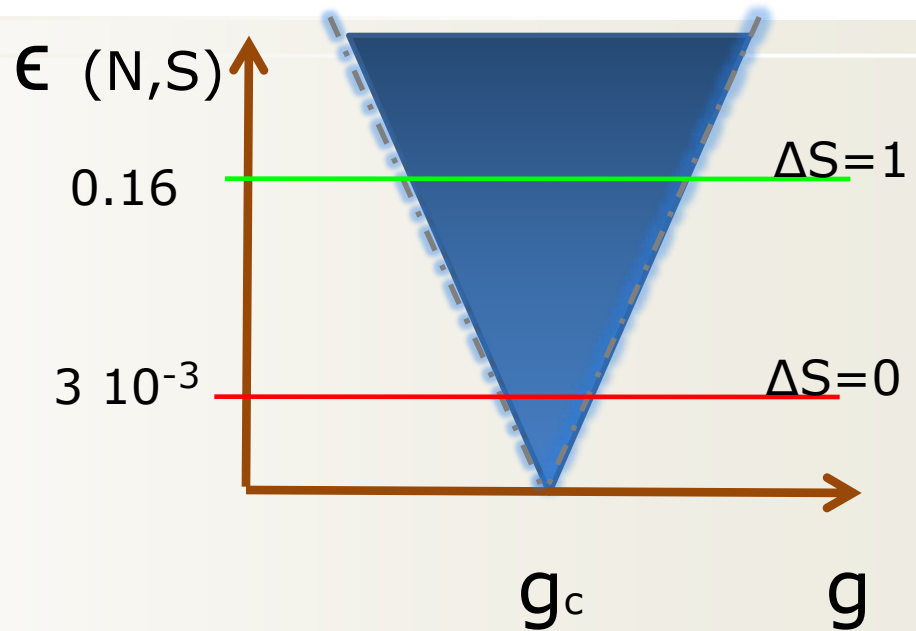
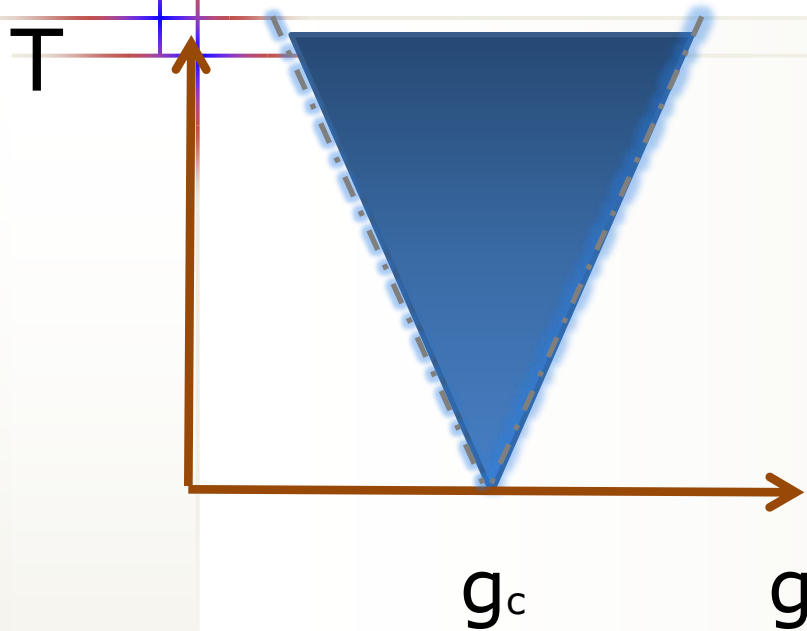


Free energy histogram



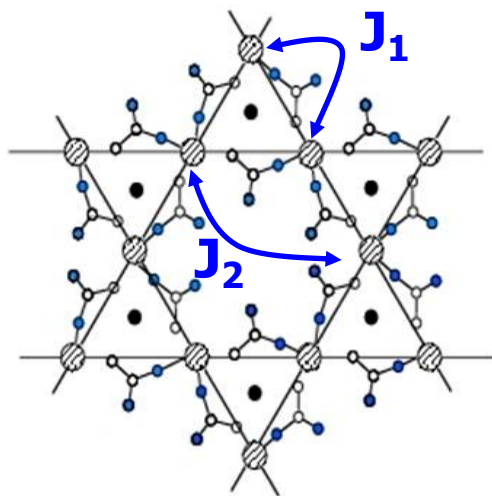
$\langle n_v \rangle$ = density of Z_2 point defects of the continuous spin texture (green colour above)

QCP and Quantum critical regime



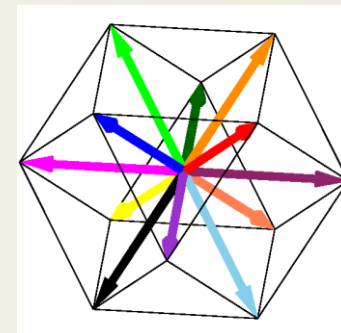
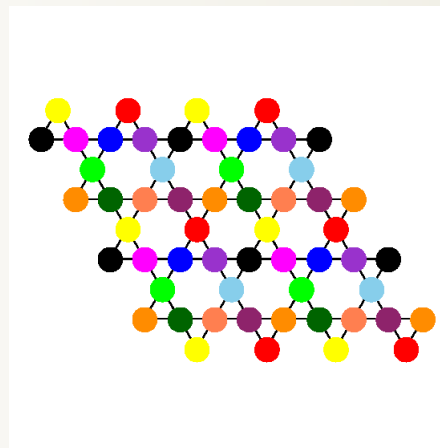
On a finite sample due to total spin quantization there is an infrared cut off to magnetic excitations that can be probed:
in the KAH pb this low energy cut off is 0.16

$\text{Cu}_3(\text{titmb})_2(\text{OCOCH}_3)_6 \cdot \text{H}_2\text{O}$ AF Heisenberg magnet on kagomé lattice?



Honda *et al.*, *J. Phys. Condens. Matter* (2002)
Narumi *et al.*, *Europhys. Lett.* (2004)

$$J_1 \sim -19\text{K} \quad J_2 \sim 6\text{K}$$



S=1/2
14.12

Liu *et al.*, *Inorg. Chem.* (1999)

Magnetization "Steps" on a Kagome Lattice in Volborthite

Hiroyuki Yoshida, Yoshihiko Okamoto, Takashi Tayama, Toshiro Sakakibara, Masashi Tokunaga, Akira Matsuo, Yasuo Narumi, Koichi Kindo, Makoto Yoshida, Masashi Takigawa
and Zenji Hiroi*

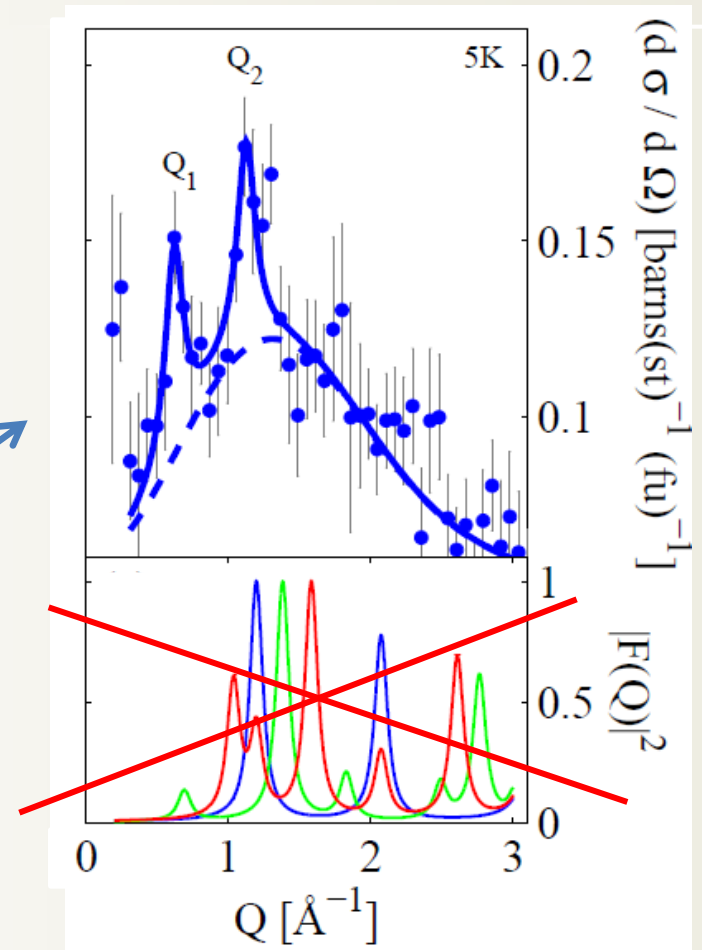
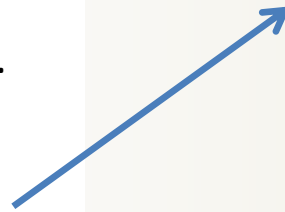
Institute for Solid State Physics, University of Tokyo, Kashiwa, Chiba 277-8581, Japan

Magnetic properties of the spin-1/2 kagome-like compound volborthite are studied using a high-quality polycrystalline sample. It is evidenced from magnetization and specific heat measurements that the spins on the kagome lattice still fluctuate at low temperature, down to $T = 60$ mK that corresponds to 1/1500 of the nearest-neighbor antiferromagnetic interaction, exhibiting neither a conventional long-range order nor a spin gap. In contrast, ^{51}V NMR experiments revealed a sharp peak at 1 K in relaxation rate, which indicates that a certain exotic order occurs. Surprisingly, we have observed three "steps" in magnetization as a function of magnetic field, suggesting that at least four liquid-like or other quantum states exist under magnetic fields.

Quantum behavior

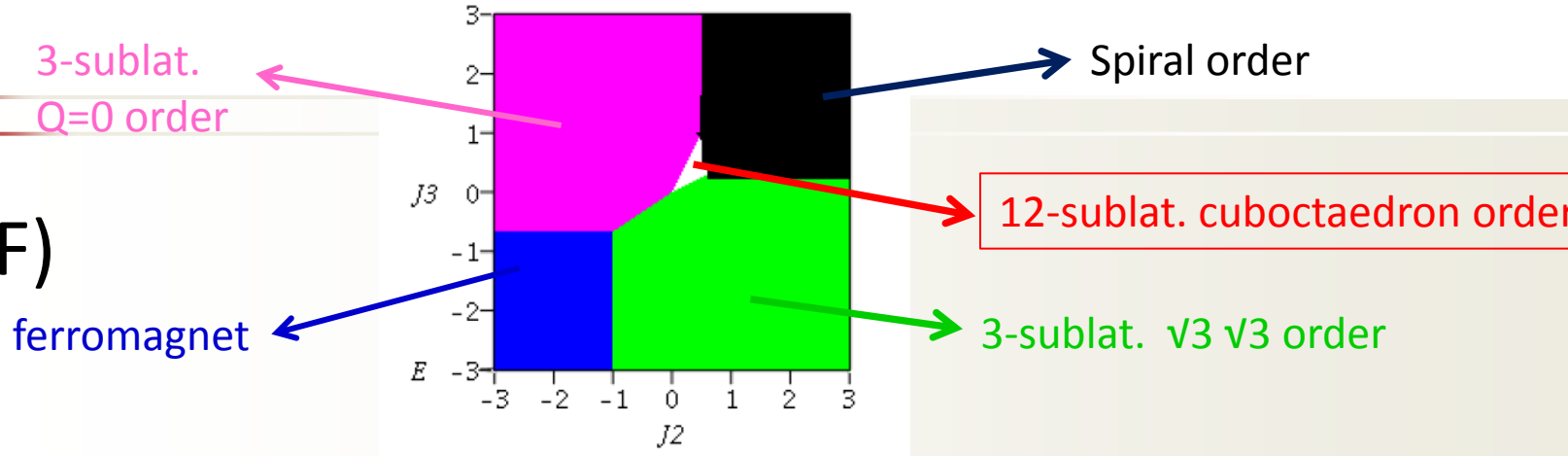
(work in progress L. Messio)

- Chiral spin liquids can exist
 - The J_1 - J_2 - J_3 models with competitive interactions on the kagome lattice
 - the MSE model on the triangular lattice
- Experimental indications of non coplanar SRO in Vollborthite
 - Z. Hiroi's group J. of Phys. Soc. Jpn 78, 2009,
 - G. Nilson & al. (EPFL 2010) arxiv:1001.2462
- & possibly Kapellasite:
 - B. Fåk & A. Wills (ILL 2010)

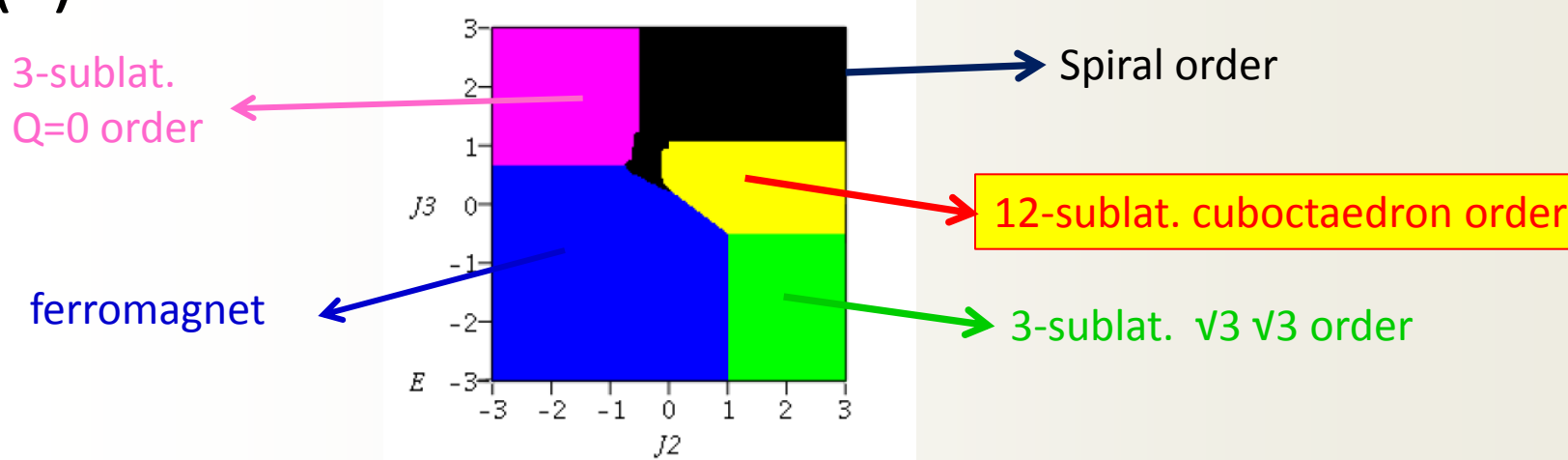


Phase diagram of the classical J_1 - J_2 - J_3 model

$J_1 = 1$ (AF)



$J_1 = -1$ (F)

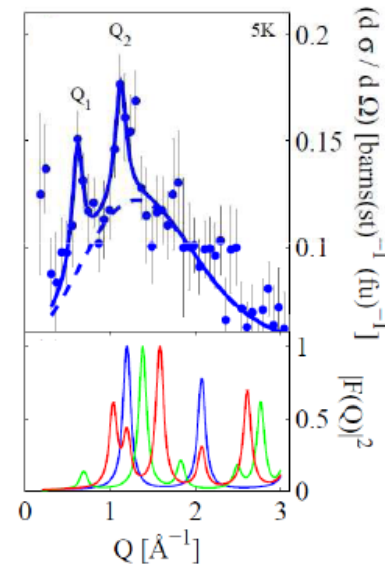
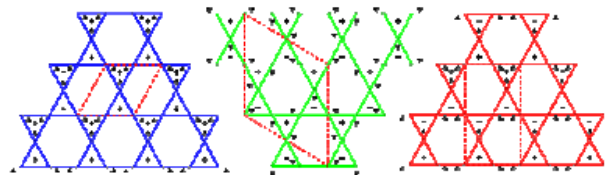


Polarized Neutron experiment

Goran Nilsen 2010

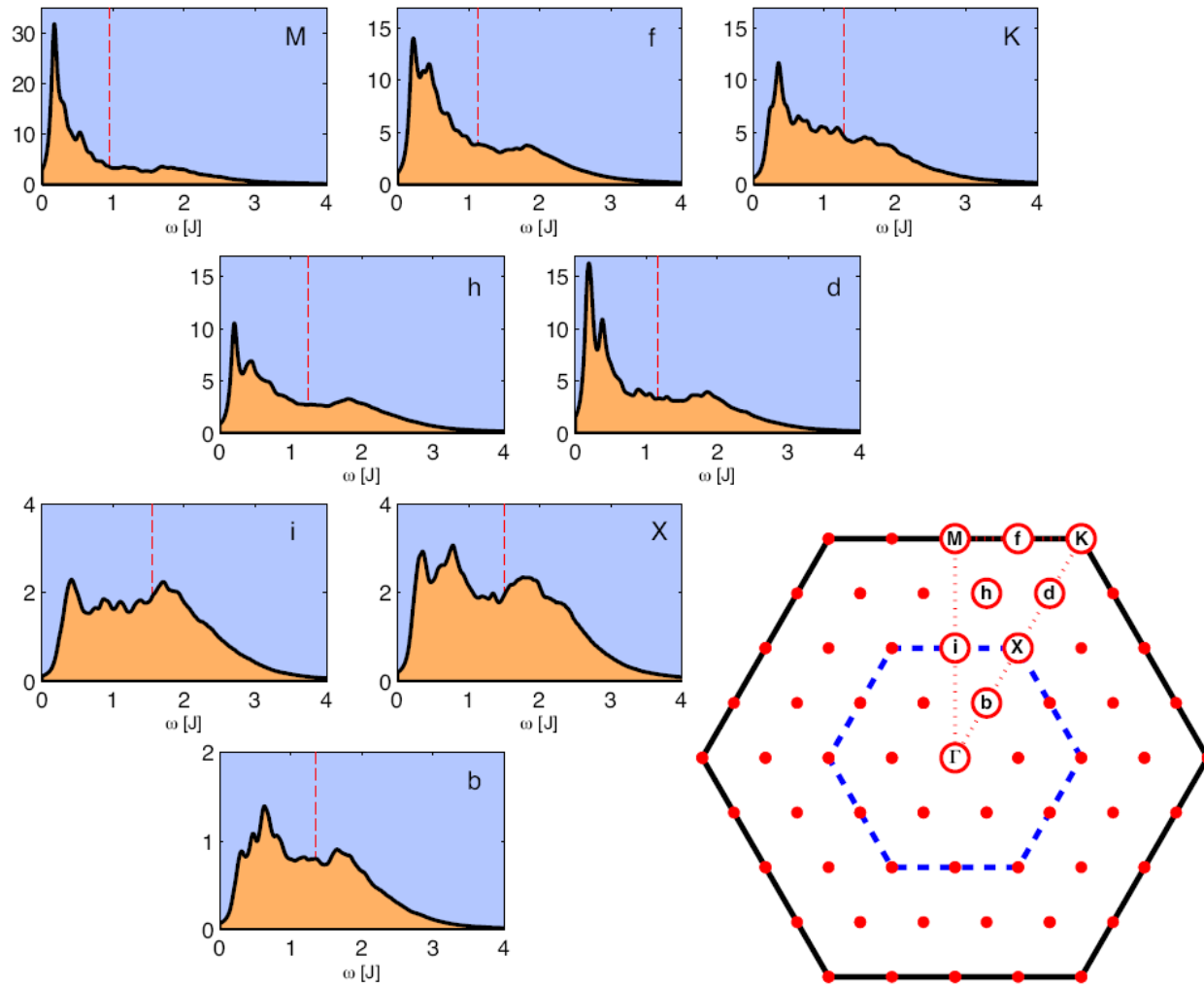
Volborthite: Polarised NS 2

- At 5K, two additional Bragg-like features appear at Q_1 and Q_2 .
- Correspond to SRO with two propagation vectors – data of insufficient quality to extract further details.
 - $\xi \sim 3r_{nn}$



Dynamical Structure Factor

Andreas Laeuchli 2007

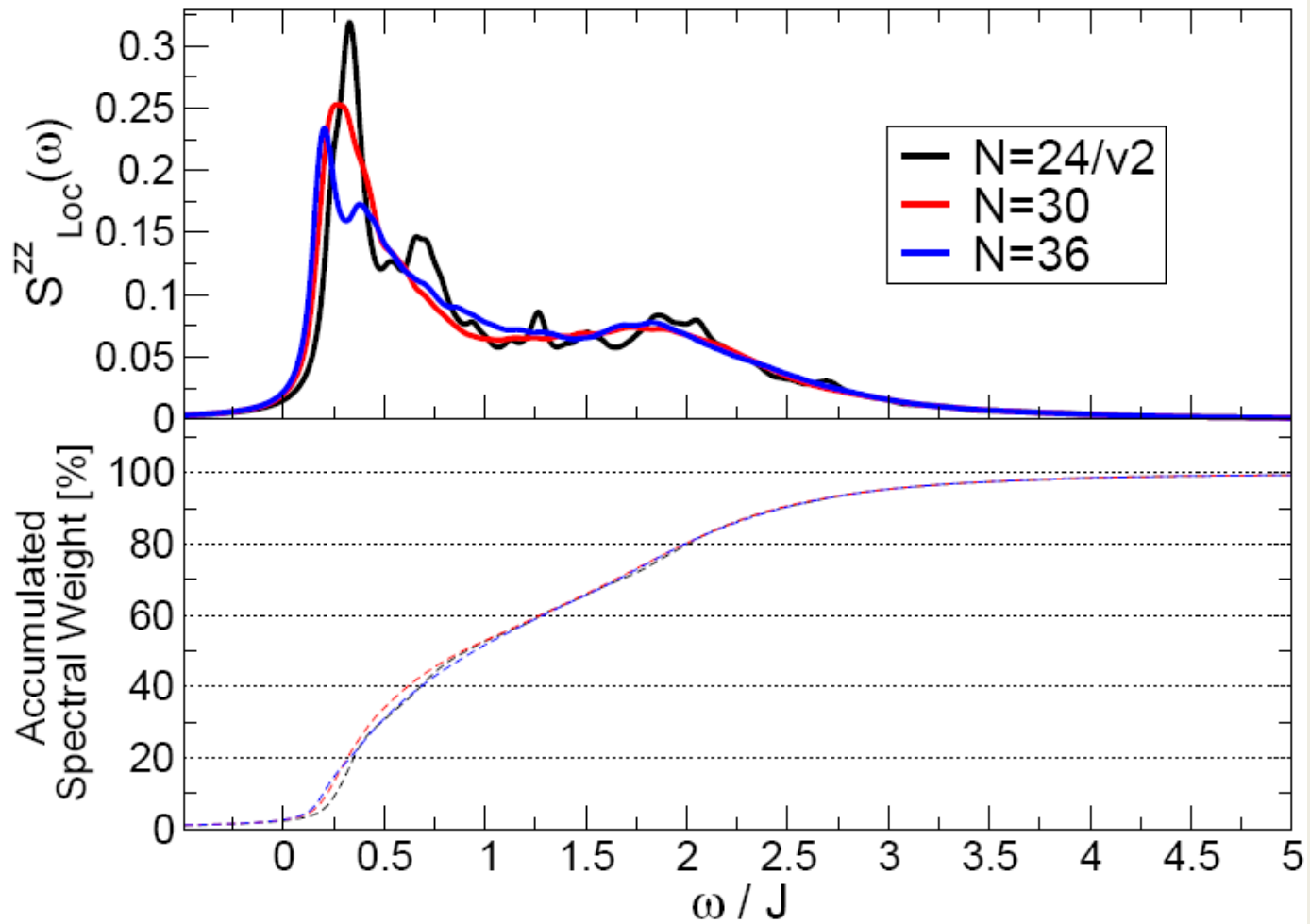


Dynamical Structure Factor

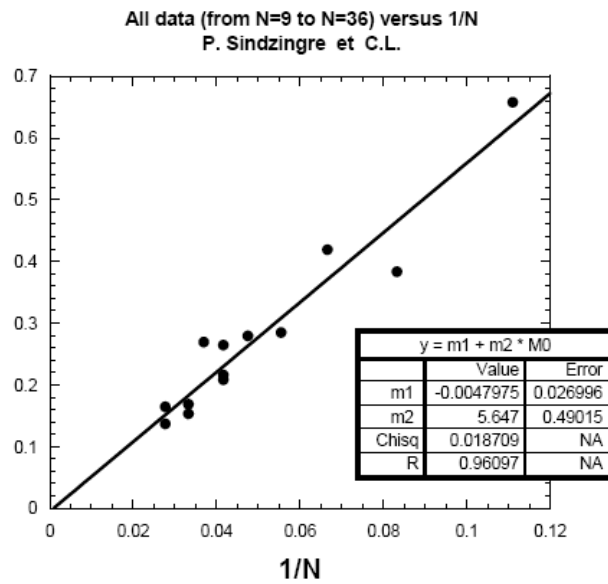
Andreas Laeuchli 2007

Kagome Local Spin Dynamics

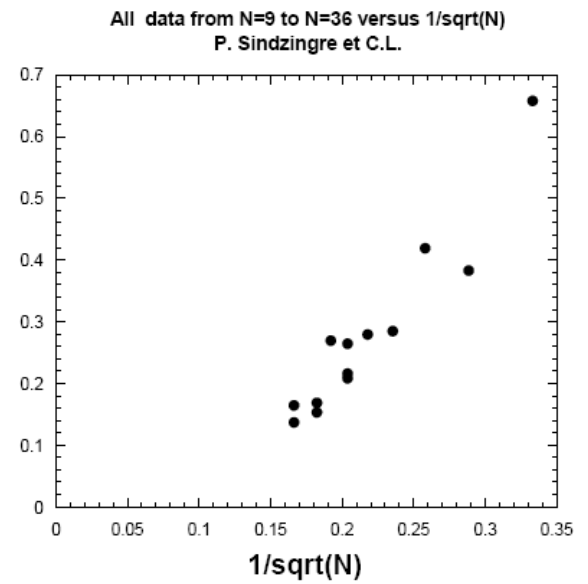
$$\eta=0.05J$$



Gap $H = \sum Si.Sj$ on kagome latt.

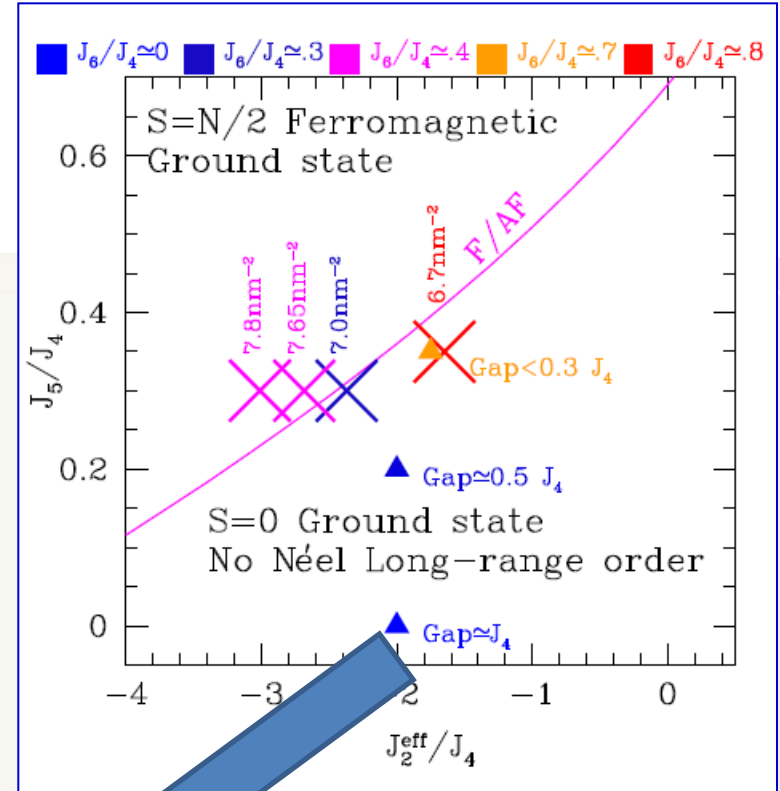


Gap $H = \sum Si.Sj$ on kagome latt.



Small digression around ^3He

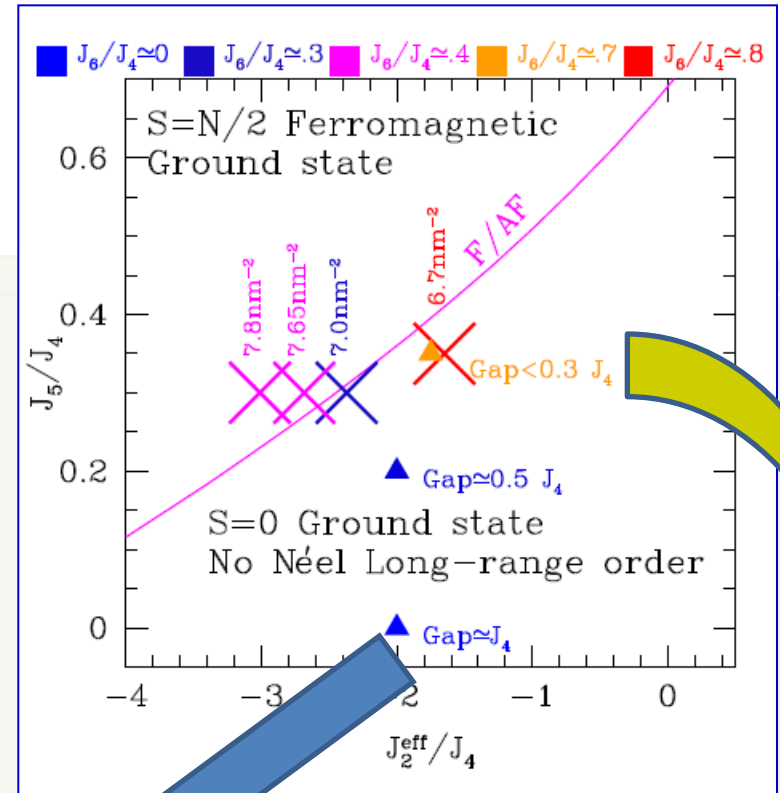
- [6] K. Ishida, M. Morishita, K. Yawata, and H. Fukuyama, Phys. Rev. Lett. **79**, 3451 (1997).
- [7] R. Masutomi, Y. Karaki, and H. Ishimoto, Phys. Rev. Lett. **92**, 025301 (2004).
- [8] E. Collin, S. Triqueneaux, R. Harakaly, M. Roger, C. Bauerle, Yu.M. Bonkov, and H. Godfrin, Phys. Rev. Lett. **86**, 2447 (2001).
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- [10] G. Misguich, B. Bernu, C. Lhuillier, and C. Waldmann, Phys. Rev. Lett. **81**, 1098 (1998).
- [11] T. Momoi, H. Sakamoto, and K. Kubo, Phys. Rev. B **59**, 9491 (1999).



Gapped Spin Liquid

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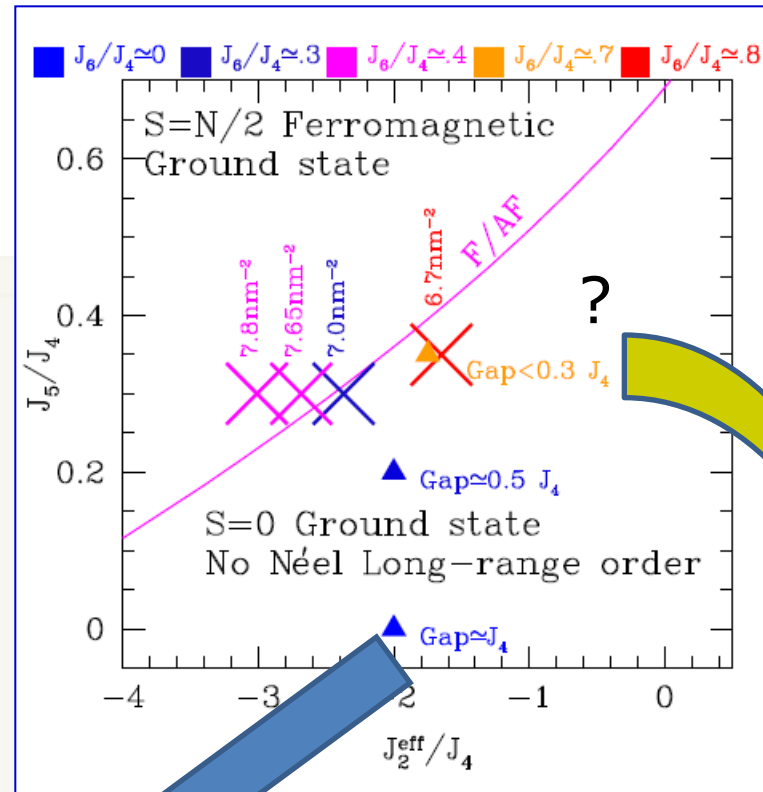


Nematic quadrupolar order near the ferromagnetic phase:
Momoi, Sindzingre, Shannon PRL 2006

Gapped Spin Liquid

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Recent measurement
of the $m=1/2$ plateau:
Nema et al. PRL 2009

Confirm the multi-spin exchange model
But would justify revisiting the
values of the coupling constants

Nematic quadrupolar order
near the
ferromagnetic phase :
*Momoi, Sindzingre, Shannon
PRL 2006*

Gapped Spin Liquid